

ADVANCED CONCEPT TRAINING Nonlinear & Stability

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Introduction

1.1. Professional training

This course will explain the nonlinear and stability calculations in SCIA Engineer. Most of the modules necessary for this calculation are included in the **Professional edition**.

For some options a concept edition is sufficient or for other options an expert edition or an extra module is required. This will always be indicated in the corresponding paragraph.

1.2. Introduction to nonlinear and stability

In the first part of this course, stability calculations will be introduced. Such a calculation determines the elastic critical buckling load of a structure. This analysis can be used to calculate the buckling length of a part of the structure or to determine whether a 2nd order analysis should be carried out.

In the second part, the course will explain how to introduce different nonlinear behaviours in a structure. First the 2nd and 3rd order calculation methods are explained and integrated with Eurocode 3. Next the local nonlinearities are examined including tension-only members, pressure-only supports, cable analysis, friction supports, etc. and finally concluded with physical nonlinearities.

Then, a small chapter will explain the integration of these nonlinear behaviours into the stability calculation.

The final chapter provides some common failure messages which occur during a nonlinear analysis. This chapter points out the most likely causes of singularities and convergence failures.

Stability Calculations

A stability calculation calculates the global buckling mode (eigenmode) of a structure under the given loading. In addition, the ratio between the buckling load and the applied load is given.

Stability calculations are used to obtain an insight into the buckling mechanisms of a structure, to calculate the buckling length of a member for use in the Steel Code Check, to verify if 2nd Order calculations are required, ...

2.1 Stability Combinations

For a stability calculation, the principle of superposition does not hold. Every combination of loads will require a separate calculation. The combinations have to be assembled before starting the calculation. In SCIA Engineer, this is done by defining **stability combinations**.



A stability combination is defined as a list of load cases where each load case has a specified coefficient.

Stability combinations		×
🏓 🤮 🗶 😒	🗠 🎒 🗳 🔒 🛛 Input	• 7
S1	Name	S1
S2 4	Contents of combination	
S3	LC1 - Self Weight [-]	1,35
S4	LC2 - Self Weight Cladding [-]	1,35
S5	LC3 - Maintenance [-]	1,50
	LC4 - Snow [-]	0,75
	3DWnd10 - 180, + CPE, - CPI [-]	0,90
New from linear combination	ns New Insert Edit	Delete Close

It is also possible to import the linear combinations as stability combinations. Choose the option **New from linear combinations**, select the desired combinations and click on close. The selected combinations will be added as stability combinations.

2.2 Linear Stability

During a linear stability calculation, the following assumptions are used:

- Physical linearity.
- The elements are taken as ideally straight and have no imperfections.
- The loads are guided to the mesh nodes, it is mandatory to refine the finite element mesh in order to obtain precise results.
- The loading is static.
- The critical load coefficient is, per mode, the same for the entire structure.
- Between the mesh nodes, the axial forces and moments are taken as constant.

The equilibrium equation can be written as follows:

$$[K_{\rm E} - K_{\rm G}] \cdot u = F$$

The symbol **u** depicts the displacements and **F** is the force matrix.

As specified in the theory of the Timoshenko method, the stiffness K is divided in the elastic stiffness K_E and the geometrical stiffness K_G . The geometrical stiffness reflects the effect of axial forces in beams and slabs.

The basic assumption is that the elements of the matrix K_G are linear functions of the axial forces in the members. This means that the matrix K_G corresponding to a λ^{th} multiple of axial forces in the structure is the λ^{th} multiple of the original matrix K_G .

The aim of the buckling calculation is to find such a multiple λ for which the structure loses stability. Such a state happens when the following equation has a non-zero solution:

$$[K_{\rm E} - \lambda \cdot K_{\rm G}] \cdot u = 0$$

In other words, such a value for λ should be found for which the determinant of the total stiffness matrix is equal to zero:

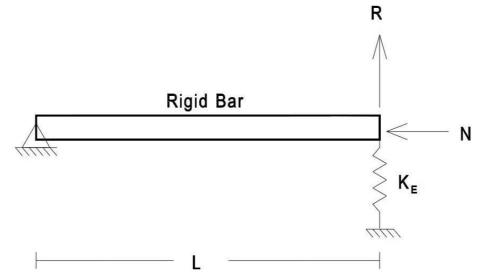
$$K_E - \lambda \cdot K_G = 0$$

Similar to the natural vibration analysis, the subspace iteration method is used to solve this eigenmode problem. As for a dynamic analysis, the result is a series of **critical load coefficients** λ with corresponding eigenmodes.

2.3 Manual calculation of K_G

The principle of a stability calculation and the meaning of the matrix ${\bf K}_{\rm G}$ will be explained with a simple example.

Suppose the next situation:



This beam with length L has a pinned support at the left and a flexible spring support at the right with rigidity: K_{E} .

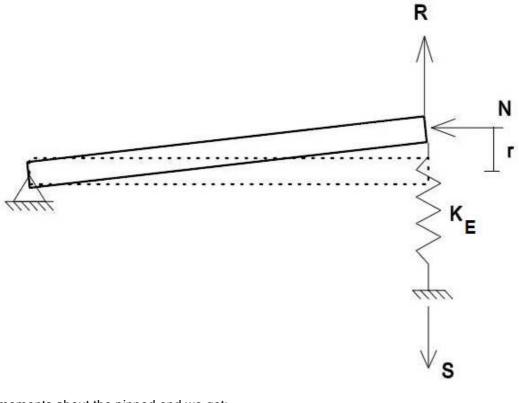
Two point loads are inputted on the beam: a vertical R and a compression force N.

Standard analysis says that R and N are independent (in the non-deformed configuration) and the stiffness relationship is:

 $K_E \cdot r = R$

With *r* the vertical translation of the right point of the beam.

But, if the structure is allowed to deform, we can calculate equilibrium in the deformed configuration as shown below:



Summing moments about the pinned end we get:

$$\mathbf{R} \cdot \mathbf{L} + \mathbf{N} \cdot \mathbf{r} = \mathbf{S} \cdot \mathbf{L}$$

The equation for the response of the spring is:

$$K_E \cdot r = S$$

Substituting S we get:

$$\mathbf{R} \cdot \mathbf{L} + \mathbf{N} \cdot \mathbf{r} = (\mathbf{K}_{\mathbf{E}} \cdot \mathbf{r}) \cdot \mathbf{L}$$

Dividing by L:

$$R + \frac{N}{L} \cdot r = K_E \cdot r$$

And grouping terms we have:

$$\mathbf{R} = (\mathbf{K}_{\mathrm{E}} - \frac{\mathbf{N}}{\mathbf{L}}) \cdot \mathbf{r}$$

This can further be re-written if we define the geometric stiffness as:

$$K_G = \frac{N}{L}$$

giving the final form as:

$$R = (K_E - K_G) \cdot r$$
$$[K_E - K_G] \cdot u = F$$

When the normal force **N** is multiplied with a factor α_{cr} so that the total rigidity becomes zero:

$$\mathrm{Ke} - \frac{\alpha_{\mathrm{cr}} \cdot \mathrm{N}}{\mathrm{L}} = 0$$

The structure will buckle and become "unstable".

Or:

2.4 Performing the calculation & examples

To perform a Stability calculation, the **stability** functionality must be activated.

	GENERAL	DI	TAILED	
	Property modifiers		Subsoil	
	Model modifiers		Pad foundation check	
	Parametric input		Steel	
-	Climatic loads		Fire resistance checks	
- 1	Mobile loads		Steel connections	
	Dunamics		Scaffolding	
	Stability 🗹		7DoF 2nd order analysis for LTB	
-	Nonlinearity		Girders with sinusoidal webs	
1	Structural model			
	IFC properties			
	Prestressing			
	Bridge design			
	Excel checks			
	Substitution beam			

The λ values can be found under the caption α **Critical load coefficients** The number of critical coefficients to be calculated per stability combination can be specified in the solver settings, as well as the solver method to be used in the calculation. Lanczos is chosen by default, because it gives fast and good results, but in some cases it will fail to find the solution. In these cases you can try the other, slightly slower, methods to obtain a result.

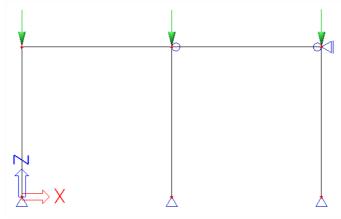
	Solver setup			×
		Name	SolverSetup1	
		Specify load cases for linear calculation		
		Specify combinations for nonlinear calculation		
	Advanced solver settings			
⊳	General			
⊳	Nonlinearity			
⊳	Initial stress			
- 4	Stability			
		Type of eigen value solver	Lanczos	*
		Number of buckling modes	4	
⊳	Soil			
			ОК	Cancel

Notes:

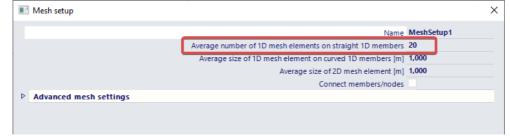
- The first eigenmode is usually the most important and corresponds to the lowest critical load coefficient. A possible collapse of the structure usually happens for this first mode.
- The structure becomes unstable for the chosen combination when the loading reaches a value equal to the current loading multiplied with the critical load factor.
- A critical load factor smaller than 1 signifies that the structure is unstable for the given loading.
- Since the calculation searches for eigen values which are close to zero, the calculated λ values can be both positive or negative.
 A negative critical load factor signifies a tensile load. The loading must thus be inversed for buckling
- to occur (which can for example be the case with wind loads).
- The eigenmodes (buckling shapes) are dimensionless. Only the relative values of the deformations are of importance, the absolute values have no meaning.
- For shell elements the axial force is not considered in one direction only. The shell element can be in compression in one direction and simultaneously in tension in the perpendicular direction. Consequently, the element tends to buckle in one direction but is being 'stiffened' in the other direction. This is the reason for significant post-critical bearing capacity of such structures.
- It is important to keep in mind that a Stability Calculation only examines the theoretical buckling behaviour of the structure. It is thus still required to perform a Steel Code Check to take into account Lateral Torsional Buckling, Section Checks, Combined Axial Force and Bending,...

Example: Buckling_Frame.esa

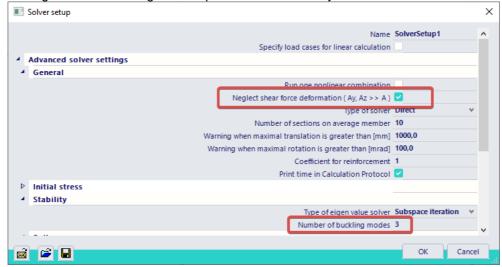
A stability analysis is performed on a steel frame. The first three buckling modes are calculated and the buckling loads are compared to the analytical results from ref.[25] to obtain a benchmark for the stability calculation of SCIA Engineer.



To obtain precise results, the number of 1D elements is refined in the mesh settings.



In the **solver setup** the **number of critical values** can be specified. In addition, the **shear force deformation** is neglected to have a good comparison with the analytical results.

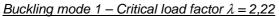


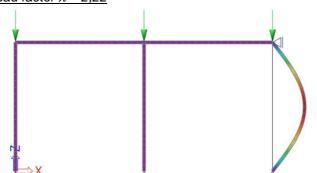
After executing a stability calculation, the following critical load coefficients are obtained:

Critical load coefficients

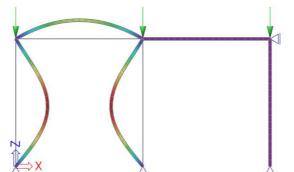
N -	f []
Stabilit	cy combination : S1
1	2,22
2	2,89
3	3,54

The corresponding buckling modes can be shown under **3D deformations** for the **stability combination**.

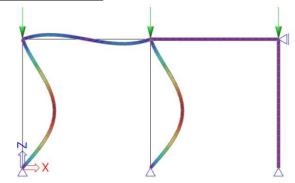




Buckling mode 2 – Critical load factor $\lambda = 2,89$



Buckling mode 3 – Critical load factor $\lambda = 3,54$



The loading F on each column is 100 kN so the critical buckling load N_{cr} can be calculated as: $N_{cr}=\lambda\cdot F$

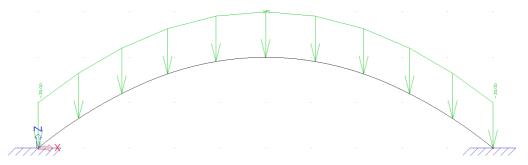
This gives the following results which can be compared to the analytical calculation:

N _{cr} for	SCIA Engineer	Ref.[25]
Buckling Mode 1	222 kN	221.5 kN
Buckling Mode 2	289 kN	289.6 kN
Buckling Mode 3	354 kN	353.8 kN

Example: Buckling_Arch.esa

When calculating for example an arched steel bridge, one of the required parameters for a steel code check is the buckling length of the arch. Using a stability calculation, the buckling factor of any member can be obtained.

As an example, a steel parabolic arch is modelled with two fixed end points. The arch has a horizontal length of **10m**, height **2m** and is loaded by a vertical line load of **30 kN/m**.



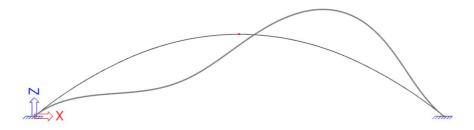
The **shear force deformation** is neglected to have a good comparison with analytical results. Using an **average mesh size on curved 1D members** of **0,1m**, a **stability calculation** yields a critical load factor of 0,46.

Mesh setup			×
	Name	MeshSetup1	I
	Average number of 1D mesh elements on straight 1D members	1	
	Average size of 1D mesh element on curved 1D members [m]	0,100	
	Average size of 2D mesh element [m]	0,100	
	Connect members/nodes		
Advanced mesh settings			
		ОК	Cancel

Critical load coefficients

N -	f []
Stabilit	y combination : S1
1	0,46
2	0,77
3	1,30
4	1,82

The first buckling mode has the following shape:



This result can be checked using an analytical formula from Ref.[27]. The critical line load for a fixed-fixed arch with height 20% of the support distance is given as:

$$P_{\rm cr} = 103.2 \frac{\rm EI}{\rm L^3}$$

With: $E = Modulus of Young = 210000 N/mm^2$ I = Moment of inertia = 6666666,67 mm⁴

L = Distance between supports = 10000 mm

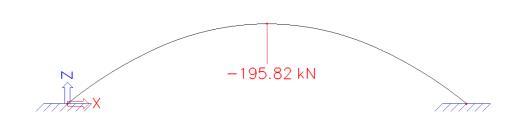
 \Rightarrow P_{cr} = 14,448 kN/m

The loading P on the structure was 30 kN/m so the critical load coefficient can be calculated as:

$$\lambda = \frac{p_{cr}}{P} = \frac{14,448 \text{ kN/m}}{30 \text{ kN/m}} = 0,48$$

This result corresponds to the result of SCIA Engineer.

Using the critical load coefficient, the buckling load of the arch can be calculated. The minimal normal force N under the given loading is **195,82 kN**. The minimal is used since this will give a conservative result for the buckling length.



The buckling load N_{cr} can then be calculated as: $N_{cr} = \lambda \cdot N = 0.46 \cdot 195.82 = 90.0772 \ kN$

Applying Euler's formula, the buckling factor **k** can be calculated:

$$N_{\rm cr} = \frac{\pi^2 \cdot E \cdot I}{(k \cdot s)^2}$$

$$\Rightarrow k = \frac{1}{s} \cdot \sqrt{\frac{\pi^2 \cdot E \cdot I}{N_{cr}}}$$

In which **s** specifies the arch length of 10,982m

The parameters can now be inputted:

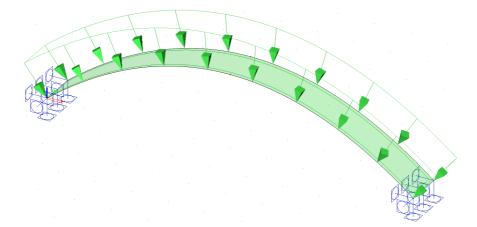
$$k = \frac{1}{s} \cdot \sqrt{\frac{\pi^2 \cdot E \cdot I}{N_{cr}}} = \frac{1}{10982 \text{mm}} \cdot \sqrt{\frac{\pi^2 \cdot 210000 \text{N/mm}^2 \cdot 6666666,67 \text{mm}^4}{90077,2N}} = 0,36$$

This buckling factor can now be inputted in the buckling data of the arch so it can be used for a steel code check.

This example illustrates the use of a stability calculation for a simple arch. The same procedure can now be applied to more complex structures like arched bridges, truss beams, concrete buildings,...

Example: Buckling_Arch_FEM.esa

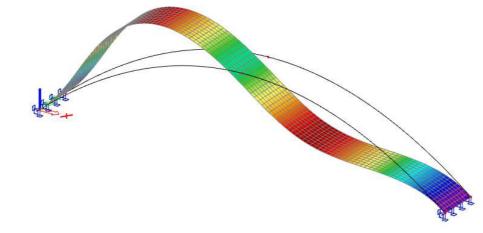
To illustrate the use of stability in finite element calculations, the arched bridge of the previous example is modelled as a shell element.



Using an average mesh size of 2D elements of 0,1m, a stability calculation yields the following critical load factor:

Critic	Critical load coefficients		
N -	f N		
Stabilit	y combination :	S1	
1	0,47		
2	0,79		
3	1,37		
4	1,92		

The corresponding buckling mode can be shown by viewing the 3D deformations



The result corresponds to the analytical solution shown in the previous example.

Example: Buckling_Arbitrary_Profile.esa

In this example, the buckling load for a composed column is calculated. The column has a variable section consisting of two different cross-sections.

The critical buckling load is compared with the analytical result from Ref.[6].

The loading is taken as **1 kN** so the critical load coefficient equals the critical buckling load. To obtain a correct comparison with the analytical calculation, the **shear force deformation** is neglected:

Solver setup		X
Nar Specify load cases for linear calculati	ion SolverSetup1	^
Advanced solver settings		
4 General		
Run one ponlinear combinati	ion	
Neglect shear force deformation (Ay, Az >>	A) 🔽	
Type of soli	ver Direct	~
Number of sections on average memb	ber 10	
Warning when maximal translation is greater than [m	nm] 1000,0	
Warning when maximal rotation is greater than (mra	ad] 100,0	
Coefficient for reinforceme	ent 1	
Print time in Calculation Proto	icol 🔽	
Initial stress		
Initial stre	ess	
4 Stability		
Type of eigen value solv	Iver Subspace iteration	n * v
	ОК	Cancel .:

The formula for the buckling load of a member with arbitrary cross-section is given in Ref.[6], pp.114 by formula (2-48):

$$P_{\rm cr} = \frac{\mathbf{m} \cdot \mathbf{E} \cdot \mathbf{I}_2}{\mathbf{l}^2}$$

With **m** a parameter depending on the length of the different sections and the ratio I_1/I_2 . This parameter is specified in table 2-10 of Ref.[6].

l ₁	8.356 10 ⁷ mm ⁴
l 2	4.190 10 ⁸ mm ⁴
а	4 m
1	10 m
a/l	0.4
I ₁ /I ₂	0.2
m	4.22
Pcr	3713 kN

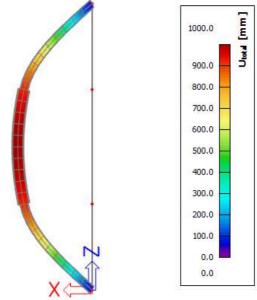
A stability calculation gives the following result:

Critical load coefficients

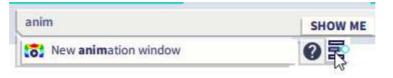
N -	f N
Stab	ility combination : S1
1	3706,75
2	8758,02
3	29795,28
4	44526.39

This result corresponds to the analytical solution.

The corresponding buckling mode has the following shape:



Note: the buckling shapes can be animated through New Animation Window



Nonlinear behavior of Structures

3.1 Type of Nonlinearity

The nonlinear behaviour of structures can be categorised in three different groups:

- Geometrical nonlinearity: the displacements are dependent on the strains in a nonlinear way.
- Physical nonlinearity: the stresses are dependent on the strains in a nonlinear way.
- Local nonlinearity: the geometry or the boundary conditions of the structure change during the solving of the equations.

These three types of nonlinearities will be examined in detail in the following chapters. For a complete overview and theoretical background, reference is made to [1], [2], [3], [4], [5] and [6].

To be able to use nonlinearities in SCIA Engineer this functionality should be enabled in the Project data dialogue:

GENERAL	DETAILED
Property modifiers	4 Nonlinearity
Model modifiers	Beam local nonlinearity
Parametric input	Support nonlinearity/basic soil spring
Climatic loads	Initial imperfections
Mobile loads	Geometrical nonlinearity
Dynamics	General plasticity
Stability	Cables
Nonlinearity 🔽	Friction support/Soil spring
Structural model	 Steel
IFC properties	Plastic hinge analysis
Prestressing	Fire resistance checks
Excel checks	Steel connections
Substitution beam	Scaffolding
	TD = F 2nd and some half for ITD

And in the right column the necessary nonlinearity should be activated.

3.2 Nonlinear Combinations

During a linear analysis, the principle of superposition is valid: the load cases are calculated and the combinations are composed after the calculation.

For a nonlinear analysis, this principle is not valid anymore. The combinations have to be assembled before starting the calculation. In SCIA Engineer, this is done by defining **nonlinear combinations**.



A nonlinear combination is defined as a list of load cases where each load case has a specified coefficient.

Nonlinear combina	tions	×	
🔎 🏪 🏒 📑 📐	🖸 😂 付 All	• V	
NC1	Name	NC1	
NC2	Description		
NC3	Solver index	(0)	
NC4	Туре	Ultimate Y	
NC5	4 Contents of combination		
NC6	LC1 - Self Weight [-]	1,35	
NC7	LC2 - Self Weight Cladding [-] 1,35		
NC8	LC3 - Maintenance [-] 1,50		
NC9	LC4 - Snow [-]	0,75	
NC10	3DWnd10 - 180, + CPE, - CPI [-]	0,90	
NC11	Bow imperfection	None Y	
NC12	Global imperfection	None Y	
NC13			
NC14			
NC15			
NC16			
NC17			
NC18			
New from combination	New Insert Edit Delet	Close	

The type of the combination, **Ultimate** or **Serviceability**, will determine what type of code check (ULS or SLS) can be performed for the specified combination.

It is important to keep in mind that as each combination requires its own calculation, no sub-combinations can be generated for a nonlinear calculation. This means that the options 'envelope' or code combinations are not available. It is however possible to generate all the required nonlinear combinations based on the existing combinations for the linear calculation. This can be done using the **New from combination** button.

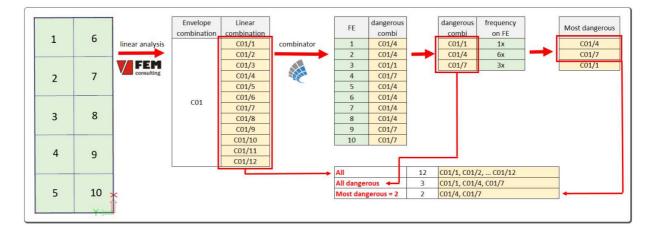
🔎 🤮 🗶 🖬 💺	≌ ⊡ ⊜	Make selection	5		×
NC1		Type of combination		Linear	Y
NC2		Used filter			
NC3		used litter		All	
NC4					
NC5	 Conte 				
NC6		Available		Selected	
NC7	LC2 -				
NC8					
NC9					
NC10	3DWn		>		
NC11					
NC12			>>		
NC13					
NC14			<<		
NC15			1		
NC16			<		
NC17	1	·			
NC18					
New from combinatio	n New I				
			Nonlin	ear combinations	: 0
	1			ate class	

In this window we first need to specify the type of combination to import, linear, or an envelope or Eurocode combination. The difference between both is that a linear combination will only create one nonlinear combination, but the other types could generate multiple combinations. The number of nonlinear combinations that will be generated for the selection is displayed on the bottom left.

When choosing for the envelope type, the filter option becomes available. This option can be very interesting when a big amount of combinations are being generated. A lot of combinations that each require a separate calculation can lead to very long calculation times. To limit this, the filter offers the following options:

Make selection	×
Type of combination Used filter	Envelope Y All All All All dangerous Most dangerous
Available	Selected
CO2 CO3	CO1 >> << <
	Nonlinear combinations: 142
	Create class
	OK Cancel

- **All** = the number of nonlinear combinations equal the number of linear combinations in the envelope combination
- All dangerous = a dangerous combination is one that creates an extreme effect in some member in the structure. That extreme effect can be an internal force or stresses in the extreme fibers of the section. Linear results will be used in order to estimate which members are getting these extreme effects. These are however based on linear results, so be careful as these aren't necessarily all the dangerous ones in terms of the nonlinear calculation.
- **Most dangerous** = it is possible to specify how many dangerous combinations are considered. This can be useful when you want to run a quick analysis with a lower amount of dangerous combinations. However, the safer option is to use the filter for all dangerous combinations and the safest is to use all.



Notes:

- The combinations defined as linear combinations can be imported as nonlinear combinations. It is however important to keep in mind that during a nonlinear calculation no combinations are generated. This implies for example that code specific combinations must first be exploded to linear combinations. These linear combinations can then be imported as nonlinear combinations. This method makes sure that the code coefficients and relations between the load cases are correctly taken into account for the nonlinear calculation.
- To view the extreme results for the nonlinear calculation, the nonlinear combinations can be grouped within a result class.
- The amount of nonlinear combinations is limited to 1000.

3.3 Calculation methods & settings

In the solver settings, different methods can be found for the execution of the calculation method as well as different settings for the calculation.

	Solver setup		\times
		ne SolverSetup1	^
	Specify load cases for linear calculation		
	Specify combinations for nonlinear calculation	on	
	Advanced solver settings		
⊳	General		
1	Nonlinearity		
	Method of calculation		1
		ts Newton-Raphson	15
	Maximum iteratio	Modified Newton-Ra Picard	aphson
	Solver precision rat	io Picard and Newton F	Raphso
	Solver robustness rat	io 1	
- 4	Initial stress		
	Initial stre	ss	
- 4	Stability		
	Type of eigen value solv	er Lanczos	*
	Number of buckling mod	es 4	
			Y
R		ОКСа	ncel

3.3.1 Solver settings

In a nonlinear calculation, it is no longer possible to compute a solution for the structure in one single step. Instead the calculation will be an iterative procedure. In each iteration the software will make a guess at the solution and then evaluate if this guess is accurate enough to considerate as a solution. If not, another iteration will be calculated until the required accuracy is reached and the guess is accepted as the final solution. How the guesses are made depends on the chosen calculation method, which will be explained over this chapter. First, let us discuss the other solver options:

- **Number of increments**: For the sake of robustness or accuracy it can sometimes be advisable to apply the loading in smaller steps (or load increments) instead of all at once. If a higher number than 1 is entered here the load will be divided into steps, and an equilibrium will be searched for the first load step before adding on the next piece of loading, until the entire load is added and the final solution is reached.
- **Maximum iterations**: As mentioned before, the solver will iterate until the required accuracy is reached and only then stop its calculation. However it may be that the loading diagram has no solution, or that the chosen calculation method is not adequate and will need a huge amount of iterations before ever reaching a solution. To prevent being stuck in extremely long calculations you can limit the maximum number of iterations here.
- Solver precision ratio: This parameter controls how the solver decides if the result of an iteration is accurate enough to stop the calculation. The convergence criterium is the following, with i the results of the current iteration and i-1 the result of the previous iteration:

$$\frac{\sum (u_{x,i}^2 + u_{y,i}^2 + u_{z,i}^2) - \sum (u_{x,i-1}^2 + u_{y,i-1}^2 + u_{z,i-1}^2)}{\sum (u_{x,i}^2 + u_{y,i}^2 + u_{z,i}^2)} \le 0,005/[solver \ precision \ ratio]$$

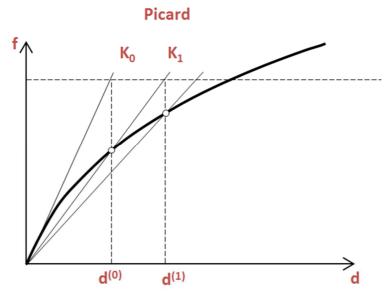
A coefficient value higher than 1 means that the tolerances will be smaller, hence the calculation will be more accurate. A coefficient value lower than 1 means that the tolerances will be larger, hence the convergence will be achieved more easily. In some case of heavy nonlinearity (e.g. cable or

membrane structures), it might be necessary to use less strict convergence criteria (e.g. ratio = 0.1) to allow for proper convergence of the analysis. Note that even with a ratio = 0.1, the convergence criteria remain very tight.

• Solver robustness ratio: This parameter affects the damping (speed of change) of the stiffness and internal forces of nonlinear hinges, supports, members. It is not possible to exactly describe it, because it is always a little different in different cases and types. It influences the convergence of nonlinear calculation with local nonlinearities on 1D members, hinges and with nonlinear surface support independently on selected method of calculation. A high value of this parameter ensures a more stable but slower convergence of the calculation. It can help in case of sensitive nonlinear analysis where convergence is problematic. A more detailed explanation can be found in the final chapter of this manual.

3.3.2 Picard

The default calculation method is the Picard method. It uses a secant line to predict possible solutions for an equilibrium. It is quite fast for basic nonlinearities (f.e. tension only elements, pressure only supports) and uses only one force increment. The method is very robust, but a bit slower than the other options. It is a good alternative for when the Newton-Raphson method fails.



For big calculations it can be interesting to combine the methods and use the Picard method for its robustness in the first few iterations, but increase the speed by using Newton-Raphson in the following iterations. This can be done by choosing 'Picard and Newton-Raphson' and then inputting how many iterations should first be performed using Picard:

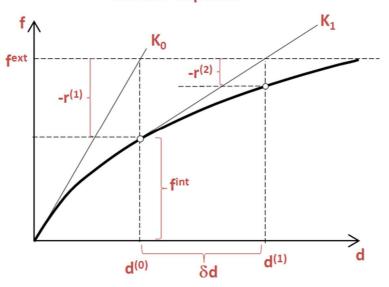
Solver setup			×
	Number of sections on average member	10	^
	Warning when maximal translation is greater than [mm]	1000,0	
	Warning when maximal rotation is greater than [mrad]	100,0	
	Coefficient for reinforcement	1	
	Print time in Calculation Protocol		
A Nonlinearity			
	Method of calculation	Picard and Newton I ¥	
	Number of increments	1	
	Maximum iterations of Picard method	1	
	Maximum iterations	50	
	Solver precision ratio	1	
	Solver robustness ratio	1	
Initial stress			
	Initial stress		
4 Stability			
	Type of eigen value solver	Lanczos v	~
		·	
		OK Cance	9

3.3.3 Newton-Raphson

The Newton-Raphson method makes its guesses for the equilibrium solution by computing the stiffness matrix of the structure in each step. This means that the iterations themselves will be slower, but the guesses will be much better. Therefore, it will require just a few iterations to find equilibrium. This method is robust for most of problems, but may fail in the vicinity of inflection points in the loading diagram. It can provide a solution even for extremely large deformations. The accuracy of the method can be increased through refinement of the finite element mesh or by increasing the number of increments. For good results this method requires at least 4 subdivisions per 1D member.

If a structure has large rotations, care should be taken to not exceed 5° of rotation per load increment.

In some specific cases a high number of increments may solve even problems that tend to a singular solution which is typical for the analysis of post-critical states.

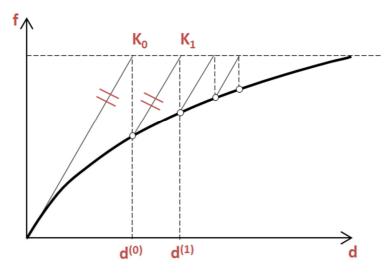


Newton-Raphson

3.3.4 Modified Newton-Raphson

This method is very similar to the Newton-Raphson method, with the only difference that the stiffness of the structure is only computed in the first iteration. The same stiffness is then used for all the other iterations, making them faster but less efficient than their non-modified version. This method can be especially interesting for very large structures, where computing the stiffness matrix in every step would lead to very high calculation times. It can also prove to be more robust in passing inflection points in the loading diagram. It also requires at least 4 subdivisions per 1D member.





Geometrical Nonlinearity – also possible with Concept edition

The options described here for the geometrical nonlinearities are also possible with a **Concept edition**. So the Professional edition is not required for this chapter, except for the stability calculation (and the calculation of α_{cr} as explained in the first chapter).

For geometrical nonlinearities, the nonlinear behaviour is caused by the magnitude of the deformations. Take for example a simple beam: during a linear analysis, the relative deformation of the end nodes, in the direction of the beam axis is dependent on the strain of the beam. Due to a curvature of the beam, the distance between the end nodes is changed. This implicates that the total strain is now not solely dependent on the displacement.

This relation can now be looked upon for different cases:

- a) Small displacements, small rotations and small strains;
- b) Large displacements, large rotations and small strains;
- c) Large displacements, large rotations and large strains;

In SCIA Engineer, methods a) and b) have been implemented for the analysis of geometrical nonlinear structures. Method c) with large strains is less common in structural applications (for example rubber) and not present in SCIA Engineer.

Method a) will be calculated with a 2nd order calculation method, like Timoshenko; method b) with a 3rd order method. An explanation about the methods and their workings is given at the end of this chapter. A 1st order method is used when geometrical nonlinearities are not taken into account.

To activate the Geometrical Nonlinearity, the functionality **Nonlinearity > Geometrical nonlinearity** must be activated.

	GENERAL	D	ETAILED	
11	Property modifiers	<u> </u>	Nonlinearity	
	Model modifiers		Beam local nonlinearity	
	Parametric input		Support nonlinearity/basic soil spring	
	Climatic loads		Initial imperfections	
- 1	Mobile loads		Geometrical nonlinearity	2
	Dynamics		General plasticity	
	Stability		Cables	
	Nonlinearity		Friction support/Soil spring	
	Structural model		Subsoil	
	IFC properties		Pad foundation check	
	Prestressing		Steel	
	Bridge design		Plastic hinge analysis	
	Excel checks		Fire resistance checks	
	Substitution beam		Steel connections	
Statistics of			Scaffolding	
			7DoF 2nd order analysis for LTB	
In Column Same 27			Girders with sinusoidal webs	

4.1. Overview

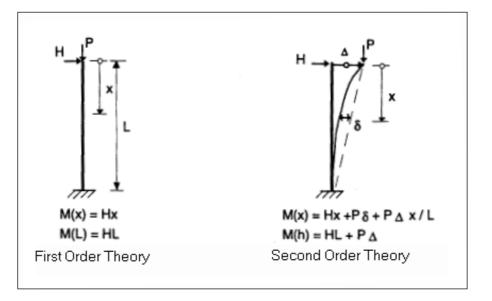
Global analysis aims at determining the distribution of the internal forces and moments and the corresponding displacements in a structure subjected to a specified loading.

The first important distinction that can be made between the methods of analysis is the one that separates elastic and plastic methods. Plastic analysis is subjected to some restrictions.

Another important distinction is between the methods, which make allowance for, and those, which neglect the effects of the actual, displaced configuration of the structure. They are referred to respectively as **second-order theory and first-order theory** based methods.

The second-order theory can be adopted in all cases, while first-order theory may be used only when the displacement effects on the structural behavior are negligible.

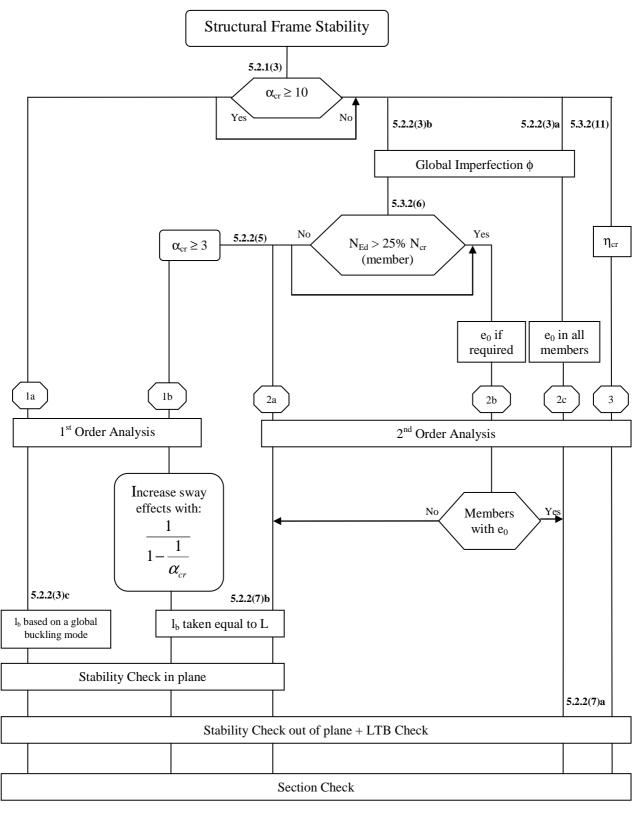
The second-order effects are made up of a local or member second-order effects, referred to as the P- δ effect, and a global second-order effect, referred to as the P- Δ effect.



On the next page an overview of the global analysis following the EN 1993-1-1, chapter 5, will be given:

- All the rules in this overview are given in the EN 1993-1-1 art. 5. For each step the rule will be indicated. The first rule (□cr > 10) will be explained in EN 1993-1-1 art. 5.2.1(3).
- In this overview 3 paths are defined:
 - Path 1: In this path a first order calculation will be executed
 - Path 2: In this path a second order calculation will be executed with global (and bow) imperfections.
 - Path 3: In this path a second order calculation will be executed with the buckling shape of the construction as imperfection.
- The calculation will become more precise when choosing for a higher path.
- The lower paths will result in a faster calculation, because a first order calculation can be executed without iterations, but this first-order theory may be used only when the displacement effects on the structural behavior are negligible.
- In the next paragraphs the rules in this overview will be explained.

To take into account all nonlinearities in the model, nonlinear load combinations are made.



With:

- η_{cr} elastic critical buckling mode.
- L member system length
- I_b buckling length

Path 1a specifies the so called Equivalent Column Method. In step 1b and 2a " l_b may be taken equal to L". This is according to EC-EN so you don't have to calculate the buckling factor =1. In further analysis a buckling factor smaller than 1 may be justified.

4.2. Alpha critical

The calculation of alpha critical is done by a stability calculation in SCIA Engineer.

According to the EN 1993-1-1, 1st Order analysis may be used for a structure, if the increase of the relevant internal forces or moments or any other change of structural behaviour caused by deformations can be neglected. This condition may be assumed to be fulfilled, if the following criterion is satisfied:

$$\alpha_{cr} = \frac{F_{cr}}{F_{Ed}} \geq 10$$
 for elastic analysis

With:

- α_{cr}: factor by which the design loading has to be increased to cause elastic instability in a global mode
- F_{Ed}: design loading on the structure
- F_{cr}: elastic critical buckling load for global instability, based on initial elastic stiffnesses

If α_{cr} has a value lower then 10, a 2nd Order calculation needs to be executed. Depending on the type of analysis, both Global and Local imperfections need to be considered.

EN1993-1-1 prescribes that 2nd order effects and imperfections may be accounted for both by the global analysis or partially by the global analysis and partially through individual stability checks of members.

The calculation of Alpha critical and also Path 3 from the diagram of the previous paragraph will be explained in the chapter "Stability".

Example: Imperfections2D.esa

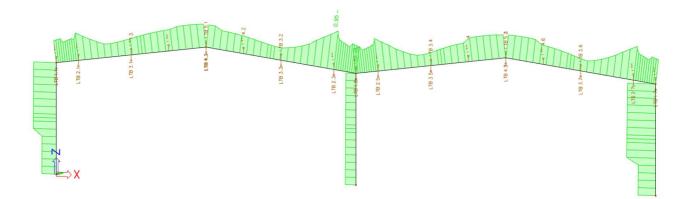
The diagram is now illustrated on a steel frame including a global imperfection. This benchmark project is examined in detail in references [19] and [22].

A stability calculation for the frame gives a critical load factor α_{cr} of **13,17 > 10**

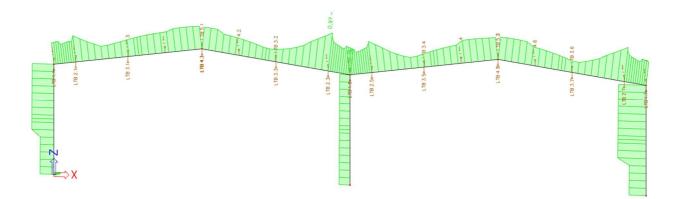
This indicates that 2nd order effects are negligible and a 1st order analysis may be used for the structure.

Path 1a can thus be followed and a 1st order calculation is executed.

A steel code check gives the following results:



When **Path 2a** is followed, using a global imperfection and a **2nd order** calculation according to **Timoshenko**, the steel code check shows the following:



It can be seen that the results are practically the same which is as expected since the α_{cr} is larger than 10.

The input of imperfections and execution of a stability calculation will be regarded in detail further in this course.

4.3. Imperfections

When performing a nonlinear calculation, it is possible to input initial geometrical imperfections: initial deformations and curvatures. These imperfections take into account the fact that the structure is for example a bit inclined instead of perfectly vertical or that the members are not completely straight.

To input geometrical imperfections, the functionality **Nonlinearity > Initial imperfections** must be activated.

Property modifiers Model modifiers Parametric input Climatic loads Mobile loads Mobile loads Dynamics Stability Nonlinearity Structural model IFC properties Prestressing Bridge design Excel checks Substitution beam Stability Pad foundation check Stability Prestressing Bridge design Substitution beam Steel connections Scaffolding TDoF 2nd order analysis for LTB Girders with sinusoidal webs	GENERAL	DETAILED
Parametric input Support nonlinearity/basic soil spring Climatic loads Initial imperfections Mobile loads Geometrical nonlinearity Dynamics General plasticity Stability Cables Nonlinearity Friction support/Soil spring Structural model 4 IFC properties Pad foundation check Prestressing Steel Bridge design Plastic hinge analysis Excel checks Steel connections Substitution beam Steel connections Stafolding TDoF 2nd order analysis for LTB	Property modifiers	A Nonlinearity
Climatic loads Mobile loads Geometrical nonlinearity Geometrical nonlinearity General plasticity General plasticity General plasticity Cables Stability Geometrical nonlinearity General plasticity General Genera	Model modifiers	Beam local nonlinearity
Mobile loads Geometrical nonlinearity Dynamics General plasticity Stability Cables Nonlinearity Friction support/Soil spring Structural model 4 IFC properties Pad foundation check Prestressing Pad foundation checks Bridge design Plastic hinge analysis Excel checks Steel connections Substitution beam Steel connections TDoF 2nd order analysis for LTB TDoF 2nd order analysis for LTB	Parametric input	Support nonlinearity/basic soil spring
Dynamics General plasticity General plasticity Cables Nonlinearity General plasticity Friction support/Soil spring Structural model IFC properties Prestressing Bridge design Excel checks Substitution beam Excel checks	Climatic loads	Initial imperfections
Stability Cables Nonlinearity Friction support/Soil spring Structural model Structural model IFC properties Pad foundation check Prestressing Pad foundation check Bridge design Plastic hinge analysis Excel checks Fire resistance checks Substitution beam Steel connections Scaffolding TDoF 2nd order analysis for LTB	Mobile loads	Geometrical nonlinearity
Nonlinearity Friction support/Soil spring Structural model IFC properties Pad foundation check Prestressing Bridge design Bridge design Plastic hinge analysis Excel checks Steel Substitution beam Steel connections Scaffolding TDoF 2nd order analysis for LTB	Dynamics	General plasticity
Structural model Subsoil Pad foundation check Prestressing Bridge design Excel checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	Stability	Cables
IFC properties Pad foundation check Prestressing Bridge design Excel checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	Nonlinearity	Friction support/Soil spring
Prestressing Bridge design Excel checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	Structural model	 Subsoil
Bridge design Plastic hinge analysis Excel checks Fire resistance checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	IFC properties	Pad foundation check
Excel checks Fire resistance checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	Prestressing	A Steel
Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB	Bridge design	Plastic hinge analysis
Scaffolding 7DoF 2nd order analysis for LTB	Excel checks	Fire resistance checks
7DoF 2nd order analysis for LTB	Substitution beam	Steel connections
		Scaffolding
Girders with sinusoidal webs		7DoF 2nd order analysis for LTB
		Girders with sinusoidal webs

📧 Nonlinear combina	tions	×
🔎 🤮 🗶 📑 💽	Ω 🗠 🎒 _All	• 7
NC1	Name	NC1
NC2	Description	
NC3	Solver index	(0)
NC4	Type	Ultimate 🗸 🗸
NC5	Contents of combination	
NC6	LC1 - Self Weight [-]	1,35
NC7	LC2 - Self Weight Cladding [-]	1,35
NC8	LC3 - Maintenance [-]	1,50
NC9	LC4 - Snow [-]	0,75
NC10	3DWnd10 - 180, + CPE, - CPI [-]	0,90
NC11	Bow imperfection	None 👻
NC12	Global imperfection	None 🔺
NC13		None
NC14		Simple inclination Inclination functions
NC15		Deform. from loadcase
NC16		Buckling shape
NC17		
NC18		
New from combination	New Insert Edit Dele	te Close

Difference is made between **Global imperfections** (Initial deformations) and **Bow Imperfections** (Curvatures).

4.3.1. Global frame imperfection φ

The nodal coordinates define the geometry of the structure. Using initial deformations as global imperfections, additional displacements (in X and Y direction) can be inputted. These displacements will thus alter the geometry.

The structure itself can therefore be modelled as straight; the inclination is given by the global imperfection.

The global imperfection can be set in the following ways:

- Simple Inclination
- Deformation from Load case
- Inclination Functions
- Buckling Shape

Simple Inclination

The imperfection is defined as a simple inclination. The inclination is defined in mm per m height of the structure. More specifically a horizontal displacement is given in the global X and/or Y direction which has a linear relation to the height (global Z direction).

Deformation from Load case

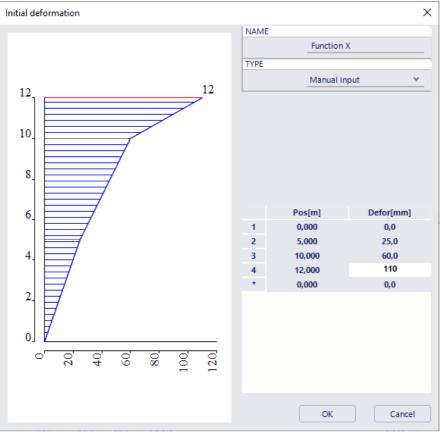
The imperfection is defined by the displacements of a specified load case. This option can be used to take into account for example the imperfections due to the self-weight. Especially for slender beams this can be important.

Inclination Functions

The imperfection is defined by a deformation-to-height curve, similar to the Simple Inclination. The curve can then be assigned to an appropriate nonlinear combination. Th

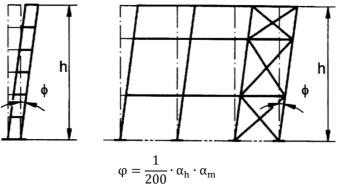
Initial deformations			?⊗
initial deformations	Ν	② 吾	
Pefinition of UCS by 3 points	W		

When the type is set to Manual input, the function can be inputted by specifying the height and the horizontal displacement.



The type Factor allows a factor to be inputted at each height. In the definition of a nonlinear combination, a manually inputted function can then be multiplied by this factor function.

When choosing **EN 1993-1-1 art. 5.3.2(3)**, the inclination function is calculated according to the code. As shown during the 2nd Order calculations, Eurocode 3 ref.[26] defines the global imperfection the following way:



With:

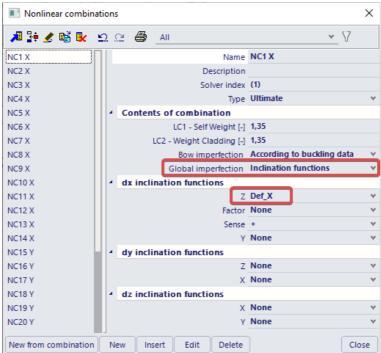
- $\alpha_h = \frac{2}{\sqrt{h}} \text{ but } \frac{2}{3} \le \alpha_h \le 1,0$
- $\alpha_m = \sqrt{0.5 \left(1 + \frac{1}{m}\right)}$
- h The height of the structure in meters
- m The number of columns in a row including only those columns which carry a vertical load N_{Ed} not less than 50% of the average value of the vertical load per column in the plane considered.

nitial deformation	
	NAME
	Function X
	ТҮРЕ
	EN 1993-1-1 art. 5.3.2(3) ¥
	BASIC IMPERFECTION VALUE : 1 /
	1 / 200
	HEIGHT OF STRUCTURE :
	m
	NUMBER OF COLUMNS PER PLANE :
	4
	OK Cancel

These parameters can be inputted after which the imperfection is automatically calculated:

Initial deformations		×
📌 🤮 🗶 🛍 🔽 🖸	2 🖨 🖨 🖬 🔤	• 7
Function X		
Name	Function X	
Туре	EN 1993-1-1 art. 5.3.2(3) v	
Basic imperfection value : 1 / [-	200,00	
Height of structure : [m]	20,000	
Number of columns per plane	4	
Φ;	0,00263500	
α _h :[-]	0,67	
α _m :[-]	0,79	
]
New Insert Edit	Delete	Close

An inclination function is defined independent of an axis. This means that the same function can be used to define the displacement in X in function of Z, or Y in function of Z, or X in function of Y, ... All of this, as well as the sign, can be defined in the nonlinear combinations.



The axis in big letters (X, Y, Z) are the axis that will be inclined. The small letter axis (dx, dy, dz) is the direction of this inclination. Generally you will only use dx-Z to incline the vertical axis in the x-direction and dy-Z to incline the vertical axis in the y-direction.

The **Sense** option allows the imperfection to be applied in the positive or negative direction (according to the chosen global direction). This way, a nonlinear combination can for example be copied, where the original has a positive sense and the copy a negative sense to take into account both possibilities.

Instead of the **Sense**, the **Factor** function can be applied as specified above. The values of the factor function will be multiplied with the values of the defined inclination function.

Buckling Shape

As an alternative to global and local imperfections, paragraph **5.3.2(11)** of Eurocode 3 Ref.[26] allows the use of a buckling shape as a unique imperfection. For this option the Professional or Expert edition is necessary.

× Project data Basic data Functionality Actions Unit Set Protection GENERAL DETAILED Property modifiers A Nonlinearity Model modifiers Beam local nonlinearity Parametric input Support nonlinearity/basic soil spring Climatic loads Initial imperfections Mobile loads Geometrical nonlinearity Dynamics General plasticity Stability 🔽 Cables Nonlinearity 🔽 Friction support/Soil spring Subsoil Structural model Pad foundation check IFC properties Steel Prestressing Bridge design Plastic hinge analysis Excel checks Fire resistance checks Substitution beam Steel connections Scaffolding 7DoF 2nd order analysis for LTB Girders with sinusoidal webs OK Cancel

To input geometrical imperfections, the functionality **Nonlinearity > Initial imperfections** and **Stability** must be activated.

Since the buckling shape is dimensionless, Eurocode gives the formula to calculate the amplitude η_{init} of the imperfection. In Ref.[28] examples are given to illustrate this method. In this reference, the amplitude is given as follows:

$$\begin{split} \eta_{\text{init}} &= e_0 \cdot \frac{N_{\text{cr}}}{E \cdot I_y \cdot \eta_{\text{cr,max}}^{"}} \cdot \eta_{\text{cr}} \\ e_0 &= \alpha \cdot \left(\bar{\lambda} - 0, 2\right) \cdot \frac{M_{\text{Rk}}}{N_{\text{Rk}}} \cdot \frac{1 - \frac{\chi \cdot \left(\bar{\lambda}\right)^2}{\gamma_{\text{M1}}}}{1 - \chi \cdot \left(\bar{\lambda}\right)^2} \text{ for } \bar{\lambda} > 0.2 \end{split}$$

With:

•
$$\bar{\lambda} = \sqrt{\frac{N_{Rk}}{N_{cr}}}$$

- α imperfection factor for the relevant buckling curve.
- χ reduction factor for the relevant buckling curve, depending on the relevant cross-section.
- N_{Rk} characteristic resistance to normal force of the critical cross-section, i.e. N_{pl,Rk}.
- N_{cr} elastic critical buckling load.
- M_{Rk} characteristic moment resistance of the critical cross-section, i.e. M_{el,Rk} or M_{el,Rk} as relevant.
- η_{cr} shape of the elastic critical buckling mode.
- $\eta_{cr,max}^{"}$ maximal second derivative of the elastic critical buckling mode.

The value of η_{init} can then be entered in the field **Max deformation**.

Nonlinear combinations				
🎜 🤮 🗶 🖄 🔛	2 😂 🗸 All	• 7		
NC1	Name NC1			
	Description			
	Solver index (1)			
	Type Ultimate	*		
	4 Contents of combination			
	LC2 - Load 1194,76 kN [-] 1,00			
	Bow imperfection None	~		
	Global imperfection Buckling shape	~		
	Stability S1	~		
	Eigen shape 1			
	Max deformation [mm] 5,7			
New from combination	New Insert Edit Delete	Close		

4.3.2. Initial bow imperfection e0

During a linear calculation, the members are taken to be ideally straight. Using bow imperfections, a local curvature can be defined for each element. A normal force in a member will thus lead to additional moments. These additional moments shall only be taken into account for members with compressive forces. To obtain correct results using bow imperfections, it is required to refine the number of **1D mesh elements**.

The local imperfection can be set in the following ways:

- simple curvature;
- according to buckling data.

SCIA Engineer will automatically apply the curvature in the following way, which is in most cases the defavourable sense:

After the first iteration step, the deflection in the middle determines the sign of the initial bow imperfection. If there is no deflection the alternating pattern is used and the beam will deform with a sinusoidal form through its nodes.

Simple Curvature

Using this option, a curvature can manually be inputted. This curvature will be used for all members in the project. This method is quite convenient when the same type of cross-section (buckling curve) is used throughout the project like for example scaffolds, framework,...

According to Buckling Data

A bow imperfection according to buckling data allows you to specify different curvatures for each used buckling data. In the **System lengths and buckling settings** properties of a member, the bow imperfection can be set, first for the span y-y and then for z-z.

System lengths and buckling settings						×
00						
	Settings Results					
	Name BC146					
	Buckling span	Deflection span				
	• y-y	Deflection z =	у-у 👻			
	z-z = z-z ¥	Deflection y =	z-z ¥			
	y-z = <u>z-z</u> ¥					
	LTB = z-z ¥					
	 Active buckling cons Span settings 	straints				
	Buckling length factors		Settings per span for y-y a	xis		
	ky factor	Calculate 💙	Sway y-y			
1	Sway y-y	Custom 👻	1	_		
	Member imperfection in 2	2nd order analysis				
	Bow imperfection e0,y	EN 1993-1-1 Table 🔺				
		From setup No bow imperfection				
		EN 1993-1-1 Table 5.1 EN 1993-1-1 Table 5.1	– plastic			
		EN 1993-1-1 Table 5.1 EN 1993-1-1 Table 5.1 Manual input of bow	– plastic – if required			
	Advanced settings	Manual input of bow	Imperrection			
	Advanced settings					
- united						
6 Q Q Q						
.40004						
			Sa	ve	Cano	el

By default the bow imperfection is set to '**From setup**'. In this case the member will follow the default setting from the steel setup:

elastic
plastic – if required nperfection
plastic elastic – if required plastic – if required

As seen during the 2nd Order calculations, Eurocode 3 Ref.[26] defines the initial bow imperfection using the following table:

EO

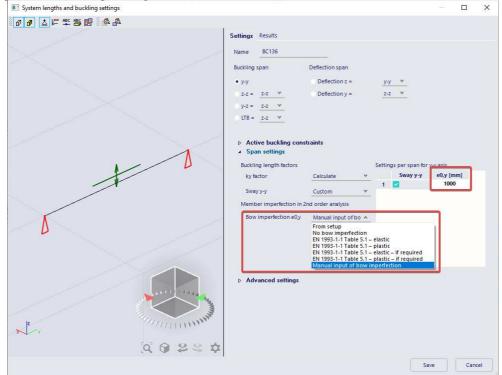
Buckling curve acc. to Table 6.1	elastic analysis e ₀ / L	plastic analysis e ₀ / L
a ₀	1 / 350	1 / 300
а	1 / 300	1 / 250
b	1 / 250	1 / 200
с	1 / 200	1 / 150
d	1 / 150	1 / 100

Where L is the member length.

When the options **EN 1993-1-1 Table 5.1 elastic/plastic** are chosen, SCIA Engineer will check the buckling curve of the member and will apply the specified imperfection automatically on the member. This imperfection is always applied which corresponds to **Path 2c** of the diagram seen during the 2nd Order calculations.

The options **EN 1993-1-1 Table 5.1 elastic/plastic** – **if required** will apply the imperfection only if the normal force N_{Ed} in a member is higher than 25% of the member's critical buckling load N_{cr} as specified in Eurocode. This corresponds to **Path 2b** of the diagram.

When selecting **Manual input of Bow Imperfection**, the imperfection can manually be inputted using the tab System lengths and buckling settings.



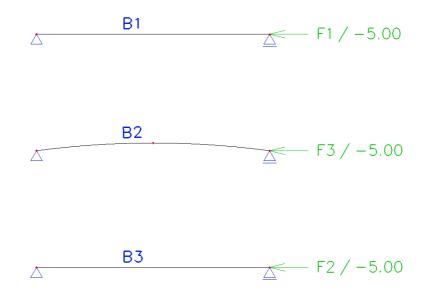
This way, the imperfection can be manually inputted for each member. This is in contrast to the **Simple Curvature** where the same bow imperfection is applied to all members.

When using bow imperfections it is important to set correct reference lengths for buckling since these lengths will be used to calculate the imperfection.

Example: Imperfection_Manual.esa

In this project, the principle of a bow imperfection is illustrated for a simple beam.

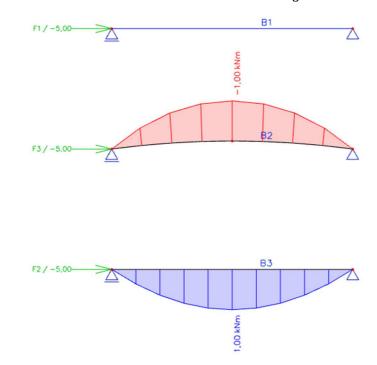
The beam is modelled once as ideally straight (**B1**). Next the beam is modelled as curved with a deflection at midpoint of 200mm (**B2**). In the third case, the beam is taken as straight and a bow imperfection of 200mm is manually set through the Buckling Data (**B3**).



The tab System lengths and buckling settings of **B3** shows the following:

? ∂ 🔺 🛱 📽 👺 📫 🐴	Colline Desuits					
	Settings Results					
	Name BC2					
	Buckling span	Deflection span				
	• y-y	Deflection z =		<u>y-y</u> *		
	Z-Z = Z-Z ¥	Deflection y =		¥		
	y-z = <u>z-z *</u>					
	LTB = <u>z-z</u> v					
	Active buckling cor	atrainte				
	Active buckling cor	istraints				
	Buckling length factors			Settings per span for	y-y axis	
BN3	ky factor	Calculate	۷	Sway y-y	e0,y [mm]	
	— F Sway y-y	Custom	¥	1	200,0	
	Member imperfection in	2nd order analysis				
	Bow imperfection e0,y	Manual input of t	00 Y 00			
	Advanced settings					
	p Auvanceu settings					
and the second						
	÷ 🌣					

The three beams are loaded by a normal force of **5** kN. Those with a deflection of 200 mm, are expected to have a moment of **1** kNm in the middle of the beam.



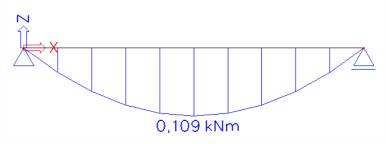
The moment diagram after a **nonlinear calculation** shows the following:

As expected, the beam B1 does not produce a bending moment. Both the curved beam and the beam with imperfection yield the 1 kNm.

This example shows that the bow imperfection corresponds to a curved calculation model.

Example: Imperfection_Self_Weight.esa

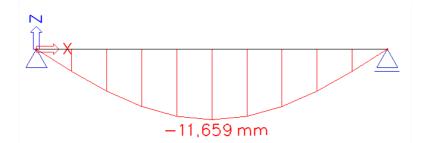
A tube on two supports is loaded by its self-weight and a compression load of 20 kN. The tube is manufactured in S235, has a cross-section RO 48,3 x 3,2 and length 5m. A **linear calculation** results in a bending moment of **0,109 kNm**:



This moment is caused entirely by the self-weight of the tube:

- Area: 453 mm² = 0,000453 m²
- Volumetric mass: 7850 kg/m³
- Length: 5m
- Loading caused by the self-weight: 7850 kg/m³ x 0,000453 m² x 9,81 m/s² = 34,88 N/m = 0,03488 kN/m
- Moment caused by the self-weight: (0,03488 kN/m x 5m x 5m) / 8 = 0,109 kNm

The self-weight causes a deformation of 11,659 mm

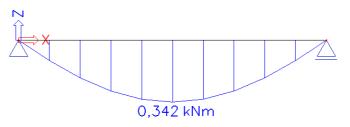


Due to the fact that the self-weight causes this deformation, the compression force of 20 kN will lead to an additional moment.

To see this effect in detail, a **nonlinear analysis** is carried out which takes into account the deflection caused by the self-weight. The deformation of the self-weight can thus be set as a **global imperfection**.

Nonlinear combinations	×
🚚 🤮 🖋 💽 😂 🖉 🔺	• 7
NC1 Name	NC1
Description	
Solver index	(1)
Туре	Ultimate v
4 Contents of combination	
LC1 - Self Weight [-]	1,00
LC2 - Compression Force 20 kN [1,00
Bow imperfection	None v
Global imperfection	Deform. from loadcase 🔹 👻
Load case	LC1 Y
New from combination New Insert Edit Delete	Close

The nonlinear calculation results in a moment of 0,342 kNm



This value can be calculated as follows:

- Imperfection due to the self-weight: 11,659mm = 0,011659m
- Compression force: 20 kN
- Additional Moment: 20 kN x 0,011659m = 0,23318 kNm
- Moment caused by the self-weight: 0,109 kNm
- → Total moment: 0,109 kNm + 0,23318 kNm = 0,342 kNm

It is clear that taking into account the deflection of the self-weight has a large influence on the results. In this example, the bending moment increases with more than 200%. Especially for slender beams the imperfection due to self-weight can be important.

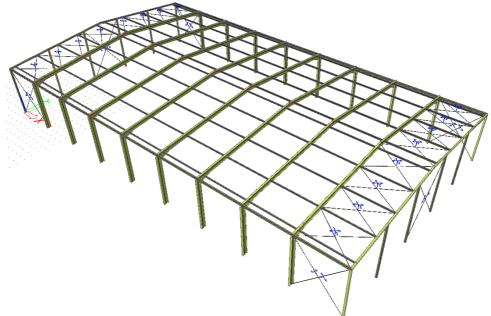
4.3.3. Example Global + Bow imperfection

In this chapter a general example of the global and bow imperfections in SCIA Engineer.

Example: Steel_Depot.esa

To illustrate the use of imperfections, both sway imperfections and bow imperfections are inputted on the columns of a steel depot.

The structure has the following layout:



The diagonals have been inputted as **tension only** members. **Inclination functions** are defined **according to the code** so the initial sway is calculated automatically:

Initial deformations		×
🏓 🤮 🗶 📸 🔍 🗠	2 🎒 🗳 🖬 🔤	• 7
Def_X		
Def_Y		
Name	Def_X	
Туре	EN 1993-1-1 art. 5.3.2(3) ¥	
Basic imperfection value : 1 / [-	200,00	
Height of structure : [m]	6,000	
Number of columns per plane	10	
Φ:	0,00302800	
α _h :[-]	0,82	
α _m :[-]	0,74	
New Insert Edit	Delete	Close

System lengths and buckling groups \times • V 🚚 🤮 🌒 🗽 🗠 🗠 🖨 💕 🔒 All 🕀 Column Name Column ~ Number of parts 1 Description Member(s) material Steel, other ky factor Factor kz factor Factor Point of load application In shear center v Mcr Calculated Bow imperfection e0,y EN 1993-1-1 Table 5.1 - elastic Y Bow imperfection e0,z EN 1993-1-1 Table 5.1 - elastic 4 SLS deflection limits Deflection limit definition From setup In plane deflection (def z) Total loads [-] 200,0 Variable loads [-] 360,0 уу ΖZ Delete New Insert Edit Close

The system lengths and buckling groups of the columns is edited to specify bow imperfections EN 1993-1-1 Table 5.1:

Since global and local imperfections are used for the columns, a buckling check needs not to be executed conform **Path 2c** of the diagram seen during the 2nd order calculations. To take this into account in SCIA Engineer, the buckling factors can be manually set to a low value so buckling will not be normative.

The Fundamental ULS combination according to Eurocode can then be imported as nonlinear combinations. The bow imperfection is set **according to buckling data** and the global imperfections are set through the **inclination functions**.

Since sway imperfections need to be considered in one direction at a time, the nonlinear combinations are taken once with the sway in X-direction and once with the sway in Y-direction.

Nonlinear combina	tions	Х
🔎 🦆 🗶 📸 💺	<u>n n 🖨 All</u>	
NC1 X	Name NC1 X	
NC2 X	Description	
NC3 X	Solver index (1)	
NC4 X	Type Ultimate	~
NC5 X	Contents of combination	
NC6 X	LC1 - Self Weight [-] 1,35	
NC7 X	LC2 - Weight Cladding [-] 1,35	
NC8 X	Bow imperfection According to buckling data	~
NC9 X	Global imperfection Inclination functions	~
NC10 X	4 dx inclination functions	
NC11 X	Z Def_X	~
NC12 X	Factor None	~
NC13 X	Sense +	~
NC14 X	Y None	~
NC15 Y	4 dy inclination functions	
NC16 Y	Z None	~
NC17 Y	X None	~
NC18 Y	4 dz inclination functions	
NC19 Y	X None	~
NC20 Y	Y None	¥
NC21 Y		
New from combination	New Insert Edit Delete Clo	ose

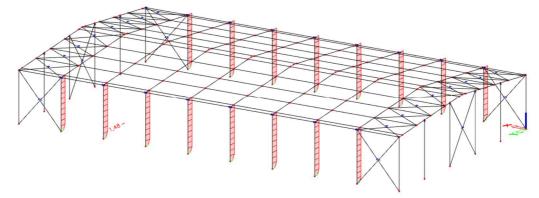
If required, this number of combinations can de doubled to change the sense of the sway imperfections.

To obtain correct results for the bow imperfections, the finite element mesh is refined.

Mesh setup			2
	Name	MeshSetup1	
	Average number of 1D mesh elements on straight 1D members	5	
	Average size of 1D mesh element on curved 1D members [m]	1,000	
	Average size of 2D mesh element [m]	1,000	
	Connect members/nodes		
Advanced mesh settings			
4 General mesh settings			
	Minimal distance between definition point and line [m]	0,001	
	Definition of mesh element size for panels	Automatic	~
	Average size of panel element [m]	1,000	
	Elastic mesh		
D 1D elements			
🛒 🖻 🔒		ОК	Cancel

A 2nd Order calculation can then be carried out using Timoshenko's method.

The Steel Code check for the mid columns yields the following result.



Since both global and local imperfections have been inputted, only the section check and the lateral torsional buckling check are relevant. In this example, member **B22** produces the largest check on the compression and bending check.

4.4. Calculation methods for geometrical nonlinearity

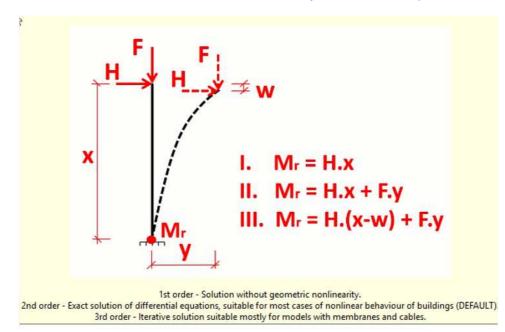
4.4.1. 2nd order: Timoshenko

For 2nd order calculations SCIA Engineer uses the so called **Timoshenko** method (Th.II.O) which is based on the exact Timoshenko solution for members with known normal force. It is a 2nd order theory with equilibrium on the deformed structure which assumes small displacements, small rotations and small strains.

When the normal force in a member is smaller than the critical buckling load, this method is very solid. The axial force is assumed constant during the deformation. Therefore, the method is applicable when the normal forces (or membrane forces) do not alter substantially after the first iteration. This is true mainly for frames, buildings, etc. for which the method is the most effective option.

The influence of the normal force on the bending stiffness and the additional moments caused by the lateral displacements of the structure (the P- Δ effect) are taken into account in this method.

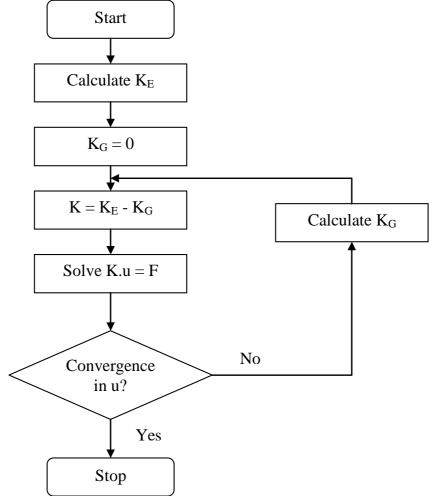
The difference between 1st, 2nd and 3rd order calculation is nicely illustrated in the picture below.



If the members of the structure are not in contact with subsoil and do not form ribs of shells, the finite element mesh of the members must not be refined.

The method needs only two steps, which leads to a great efficiency. In the first step, the axial forces are solved. In the second step, the determined axial forces are used for Timoshenko's exact solution. Further iterations are only needed if other nonlinearities are present in the structure. The original solution was generalised in SCIA Engineer to allow taking into account shear deformations.

The applied technique is the so called 'total force method' or 'substitution method'. In each iteration step, the total stiffness of the structure is adapted and the structure is re-calculated until convergence. This technique is illustrated in the following diagram.



In this figure, the stiffness \overline{K} is divided in the elastic stiffness K_E and the geometrical stiffness K_G . The geometrical stiffness reflects the effect of axial forces in beams and slabs. The symbol u depicts the displacements and F is the force matrix.

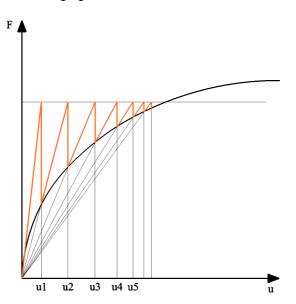
The criterion for convergence is defined as follows:

$$\frac{\sum (u_{x,i}^2 + u_{y,i}^2 + u_{z,i}^2) - \sum (u_{x,i-1}^2 + u_{y,i-1}^2 + u_{z,i-1}^2)}{\sum (u_{x,i}^2 + u_{y,i}^2 + u_{z,i}^2)} \le 0,005/(\text{precision ratio})$$

With:

- $u_{x,i}$ displacement in direction x for iteration i.
- u_{y,i} displacement in direction y for iteration i.
- u_{z,i} displacement in direction z for iteration i.

The diagram is illustrated on the following figure.



The choice of the Timoshenko Method and the maximal amount of iterations can be specified through Calculation, Mesh > Solver Setup.

•	Solver setup		×
	Name	SolverSetup1	^
	Specify load cases for linear calculation		
	Specify combinations for nonlinear calculation		
4	Advanced solver settings		
⊳	General		
4	Nonlinearity		
	Geometrical nonlinearity	2nd order (Timosher 🗸	
	Method of calculation	Picard	-
	Number of increments	1	
	Maximum iterations	50	
	Solver precision ratio	1	
	Solver robustness ratio	1	
4	Initial stress		
	Initial stress		¥
2nd	order - Solution without geometric nonlinearity. I order - Exact solution of differential equations, suitable for most cases of nonlinear behaviour of buildings order - Iterative solution suitable mostly for models with membranes and cables.	DEFAULT).	
Ř		OK Canc	el

Example: Timoshenko.esa

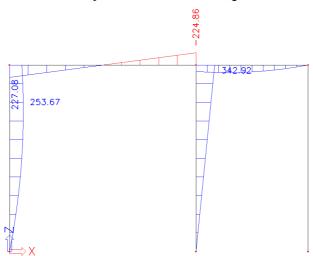
In this benchmark example, a frame is calculated both in 1st and 2nd Order using the Timoshenko method. The influence of the 2nd Order effects is seen to be significant.

The results are compared with the results from reference [7] 'Stahl im Hochbau' p256.

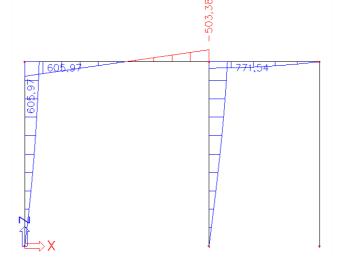
	Stahl im Hochbau	SCIA Engineer
M21	602.2 (227.1) kNm	605.97 (227.08) kNm
M32	506.0 (224.9) kNm	503.38 (224.86) kNm
M34	779.9 (343.0) kNm	771.54 (342.92) kNm

The results between brackets are those for the first order analysis.

The Moment-diagram for the 1st Order analysis shows the following:



A significant increase of the moments is seen for the **2nd Order analysis**:



4.4.2 3rd order

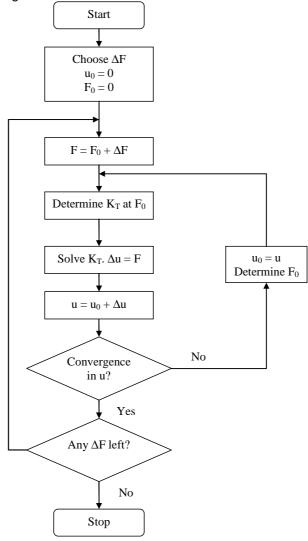
For 3rd order calculations several methods are available. Each of those iterative processes have been explained in chapter 3.3. They can be selected in the solver settings, after selecting a 3rd order calculation.

Nonlinearity		
Geometrical nonlinearity	3rd order (large deformation)	~
Method of calculation	Picard and Newton Raphson	^
Number of increments	Newton-Raphson Modified Newton-Raphson	
Maximum iterations of Picard metho	Modified Newton-Raphson Picard	
Maximum iterations	Picard and Newton Raphson	

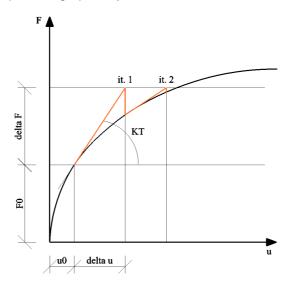
The exact process will now be explained for the **Newton-Raphson** method (Th.III.O), which is based on the Newton-Raphson method for the solution of nonlinear equations.

This method is a more general applicable method which is very solid for most types of problems. It can be used for very large deformations and rotations; however, as specified the limitation of small strains is still applicable.

Mathematically, the method is based on a step-by-step augmentation of the load. This incremental method is illustrated on the following diagram:



The following figure shows this process graphically.



In this figure, the tangential stiffness K_T is used. The symbol u depicts the displacements and F is the force matrix.

The original Newton-Raphson method changes the tangential stiffness in each iteration. There are also adapted procedures which keep the stiffness constant in certain zones during for example one increment. SCIA Engineer uses the original method.

As a limitation, the rotation achieved in one increment should not exceed 5°.

The accuracy of the method can be increased through refinement of the finite element mesh and by increasing the number of increments. By default, when the Newton-Raphson method is used, the number of **1D elements** is set to **4** and the **Number of increments** is set to **5**.

In some cases, a high number of increments may even solve problems that tend to a singular solution which is typical for the analysis of post-critical states. However, in most cases, such a state is characterized by extreme deformations, which is not interesting for design purposes.

The choice of the Newton-Raphson Method, the amount of increments and the maximal amount of iterations can be specified through **Calculation**, **Mesh > Solver Setup**.

Solver setup			
	Specify combinations for nonlinear calculation		^
Advanced solver settings			
General			
Nonlinearity			
	Geometrical nonlinearity	3rd order (large defc 🗸	
	Method of calculation	Newton-Raphson v	
	Number of increments	5	
	Maximum iterations	50	
	Solver precision ratio	1	
	Solver robustness ratio	1	
Initial stress			
	Initial stress		
4 Soil			
4 Soilin			
	Step for soil/water pressure [m]	0,500	
	Soil combination	None v	
a 🖻 🖬		OK Cance	el

As specified, the Newton-Raphson method can be applied in nearly all cases. It may, however fail in the vicinity of inflexion points of the loading diagram. To avoid this, a specific method has been implemented in SCIA Engineer: the **Modified Newton-Raphson** method.

This method follows the same principles as the default method but will automatically refine the number of increments when a critical point is reached. This method is used for the nonlinear Stability calculation and will be looked upon in Chapter 6.

In general, for a primary calculation the Timoshenko method is used since it provides a quicker solution than Newton-Raphson due to the fact Timoshenko does not use increments. When Timoshenko does not provide a solution, Newton-Raphson can be applied.

Example: N_R_Beam.esa

This project is used to illustrate the capability of the Newton-Raphson method regarding large deformations and large rotations.

The structure consists of a cantilever beam which is loaded by a moment at the free end. The rotation at the free end is given by:

$$\phi = \frac{M \cdot L}{E \cdot I}$$

When $\varphi = 2\pi$, the beam will form a complete circle. The moment required for this rotation is:

$$M_{2\pi} = \frac{2\pi \cdot E \cdot I}{L}$$

The member considered has a length of **10m** and a cross-section type **IPE200**. The parameters in this case are:

- E = 210000 N/mm²
- L = 10000 mm
- I = 1.943 107 mm4

This leads to a moment $M_{2\pi}$ =2563,73 kNm.

Since the rotation in one increment is limited to 5°, about 80 increments are needed. To obtain precise results, a dense mesh is required.

A calculation using Newton-Raphson with 80 increments and 40 mesh elements for the beam gives the following results:

Displacement of nodes

Nonlinear calculation, Extreme : Global Selection : All Nonlinear combinations : NC1

Node	Case	Ux [mm]	Uy [mm]	Uz [mm]	Fix [mrad]	Fiy [mrad]	Fiz [mrad]
N2	NC1	-9999,4	0,0	-0,4	0,0	6283,5	0,0
N1	NC1	0,0	0,0	0,0	0,0	0,0	0,0
N3	NC1	-5000,0	0,0	-3183,9	0,0	3141,6	0,0

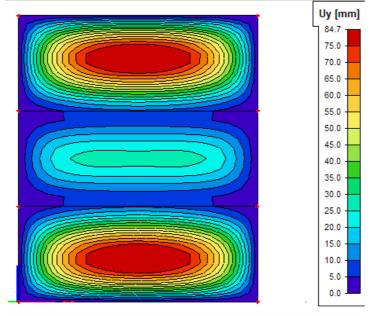
The displacement of nodes shows the following for fiy:



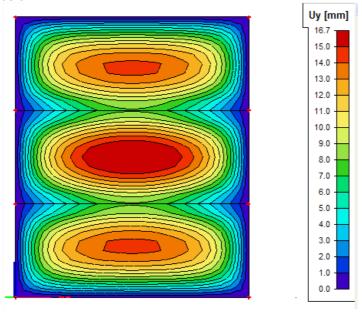
Example: N_R_Membrane.esa

This project illustrates the (positive) influence of the membrane forces on the results.

A steel plate is loaded by a surface load, perpendicular to the member system-plane. A 1st Order calculation gives the following deformations:

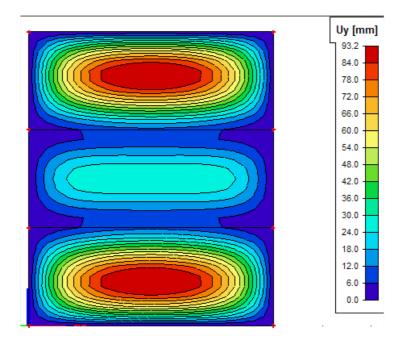


A **3rd Order** calculation using **Newton-Raphson** will take into account the development of membrane forces in the plate. These tensile membrane forces will have a positive effect on the stiffness on the plate and will thus reduce the deformations.



The results are showed below.

<u>Remark:</u> as explained before, Timoshenko is not valid for high deformations. So for this example, Timoshenko would lead to incorrect results and this method does not take into account (positive) influence of the membrane forces on the results. The deformations calculated with Timoshenko are the following:



Local Nonlinearity

The local nonlinearities can be defined for 1D members, connections between 1D members, 2D members and supports.

The following types have been implemented in SCIA Engineer:

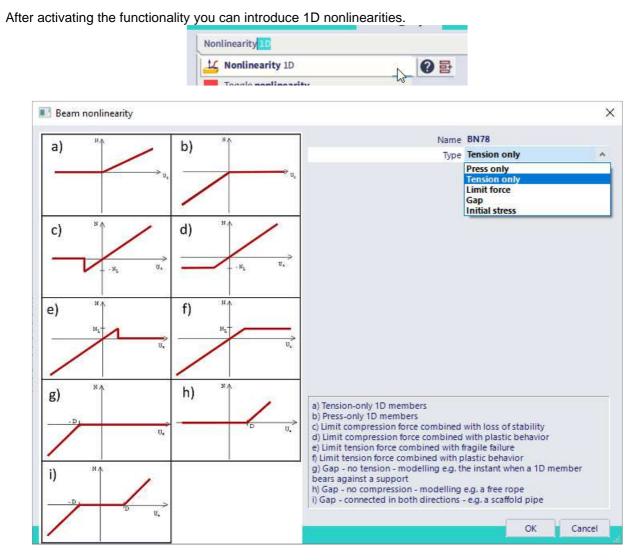
- Beam local nonlinearity;
- Beam local nonlinearity including initial stress;
- Nonlinear member connections;
- Support nonlinearity;
- Pressure only elements;
- 2D membrane elements.

5.1. Beam Local Nonlinearity – also available in the concept edition

The options described in this chapter are also possible with a **Concept edition**. So the Professional edition is not required for this chapter.

To input local nonlinearities for 1D members, the functionality **Nonlinearity > Beam local nonlinearity** must be activated.

	GENERAL	D	ETAILED
120	Property modifiers	×	Nonlinearity
	Model modifiers		Beam local nonlinearity 🗹
	Parametric input		Support nonlinearity/basic soil spring
	Climatic loads		Initial imperfections
- 1	Mobile loads		Geometrical nonlinearity
	Dynamics		General plasticity
	Stability		Cables
	Nonlinearity 🔽		Friction support/Soil spring
	Structural model		Subsoil
	IFC properties		Pad foundation check
	Prestressing		Steel
	Bridge design		Plastic hinge analysis
	Excel checks		Fire resistance checks
	Substitution beam		Steel connections
			Scaffolding
			7DoF 2nd order analysis for LTB
TAXABLE P			Girders with sinusoidal webs



The following types are available:

- Pressure only;
- Tension only;
- Limit force;
- Gap element;
- Initial stress.

All those options are explained with examples in the chapters below.

5.1.1 Members defined as Pressure only / Tension only

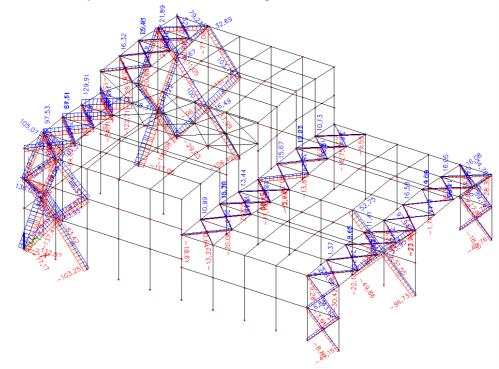
- Pressure only: the member is only active under pressure (i.e. strut, ...)
- Tension only: the member is only active under tension (i.e. anchor, diagonal, ...)

When using this type of beam nonlinearity, it can happen that numerically a very small pressure/tensile force remains in the member, mostly due to the self-weight. This value will always be negligible compared to the other force components in the member.

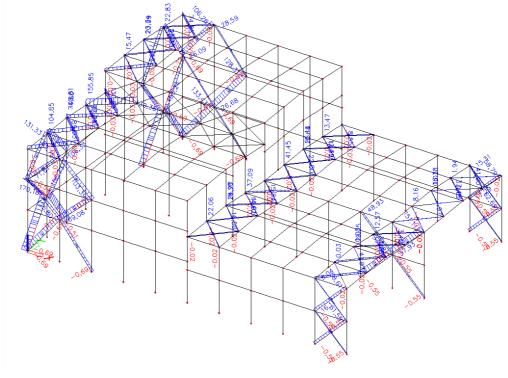
Example: Tension_Only.esa

A **3rd order** calculation is executed using **Newton Raphson**, including global imperfections. The diagonals are designated as '**Tension-only**' members.

The normal forces for a **linear analysis** show that extreme compression results are obtained in the diagonals. This will inevitably lead to failure due to buckling.



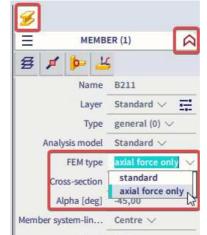
The normal forces for the **nonlinear analysis** shows that diagonals are now only subjected to tension thus buckling will not occur anymore. Only very small compression forces will appear in the diagonals.



Notes:

 It's important to keep in mind that 'Tension only' does not change anything for shear forces and moments. The only component which cannot occur is compression, but the member can still be subjected to bending, torsion, ...

To specify that a member can only be subjected to normal forces, the **FEM type** of the member can be set to **axial force only**.



When using this, you must be absolutely sure that bending effects cannot occur in reality! Also beware that **no hinges** should be added on members with axial force only, as these degrees of freedom are already free and this will lead to an instability in the calculation.

• The Calculation protocol for the Nonlinear calculation shows extra information concerning the applied nonlinearities, number of iterations per combination, ...

Calculation protocol

Nonlinear calculation

Number of 2D elements	0
Number of 1D elements	2504
Number of mesh nodes	2253
Number of equations	13518
Maximum iterations	50
Number of increments	5
Type of nonlinearity	II. order
amplied	local nonlinearities
Method (II. order)	Newton-Raphson

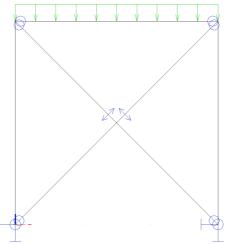
No. of combination	Start	End	No. of iterations
NC1	16.08.201808:25	16.08.201808:25	5
NC2	16.08.201808:25	16.08.201808:25	4
NC3	16.08.201808:25	16.08.201808:25	4
NC4	16.08.201808:25	16.08.201808:25	5

Example: Mechanism.esa

When using beam nonlinearities, it is important to make sure that not too many elements are eliminated.

A common error is the creation of a mechanism due to the fact too many elements have been designated tension only/pressure only and thus no solution can be found. This principle is illustrated in the following project.

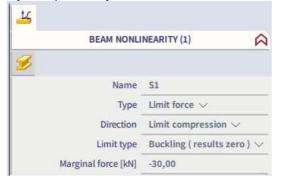
A steel frame has been modelled with hinged connections between the elements. The diagonals have been specified as **Tension only**.



Due to for example a roof load, both diagonals are subjected to compression. This is not possible for **Tension only** members so both members are eliminated causing a global instability of the frame. This can be overcome by using the modified Newton-Raphson or by inputting a very small horizontal force.

5.1.2 Members with Limit Force

A member with limit force acts in the structure until a specified limit is reached after which the member will be eliminated from the calculation or yields plastically.



The **Direction** is used to specify in which zone the limit acts: the tension zone or the compression zone.

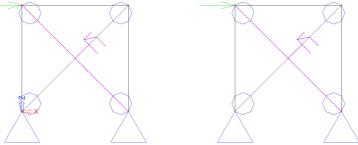
When the limit is reached, it can be specified in the **Type** field how the member should act. The member can be eliminated from the structure (**Buckling**) or the member can stay in the structure but with the limit force as maximal axial force (**Plastic yielding**).

The limit itself is defined in the field **Marginal Force**. A negative value must be specified for a compression limit and a positive value for a tension limit.

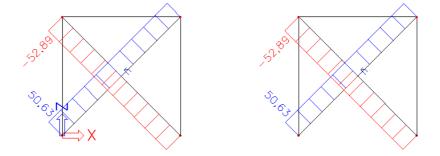
Example: Limit_Force.esa

In this project, a frame is modelled in which one diagonal has a **compression limit** of -30 kN.

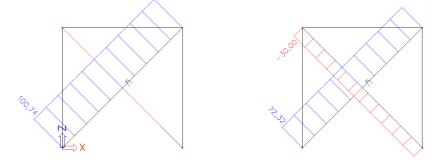
For the left frame, the type is set to **Buckling**, for the right frame the type is set to **Plastic yielding**.



A linear analysis shows the following normal forces in the diagonals of both frames:

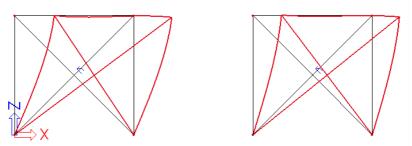


A nonlinear analysis, taking into account the limit force gives the following results for the normal forces:



In the left frame, the diagonal has buckled so the tensile force in the remaining diagonal is augmented. In the right frame, the diagonal stays in the structure but yields plastically and thus acts at the limit force of -30 kN.

The deformed structure for the nonlinear analysis shows the following:



Due to the fact one diagonal has buckled in the left frame, larger horizontal deformations occur.

5.1.3 Members with gaps

There are various connection and support conditions used in a real structure. It may happen that a beam is not attached rigidly to the structure but "starts its action" only after some initial change of its length. The beam thus has to have a certain translation in its local x-direction before it becomes active. This behaviour can be inputted using **gap** elements.



The **Type** field is used to specify if the member is active only in compression, only in tension or in both directions.

The value of the translation can be inputted in the **displacement** field. The gap can be defined at the beginning or at the end of the beam using the **position** field.

Gap members in tension only can for example be used to model a rope: the rope can only work in tension but becomes active only after a certain translation. Gap members in both directions are frequently used in scaffolding structures.

5.2. Beam Local Nonlinearity including Initial Stress

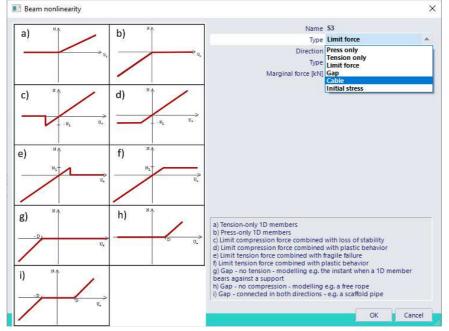
To input local nonlinearities for 1D members, including initial stresses, following functionalities must be activated:

- Nonlinearity;
- Nonlinearity > Beam local nonlinearity;
- Nonlinearity > Geometrical nonlinearity;
- Cables.

The Initial stress functionality is a standard functionality of SCIA Engineer, it is hidden and always enabled by default.

	GENERAL	D	ETAILED	_
	Property modifiers	- ×	Nonlinearity	
	Model modifiers		Beam local nonlinearity	2
	Parametric input		Support nonlinearity/basic soil spring	
	Climatic loads		Initial imperfections	
-	Mobile loads		Geometrical nonlinearity	2
	Dynamics		General plasticity	
	Stability		Cables	2
	Nonlinearity 🛃		Friction support/Soil spring	
	Structural model		Steel	
	IFC properties		Plastic hinge analysis	
	Prestressing		Fire resistance checks	
	Excel checks		Steel connections	
	Substitution beam		Scaffolding	
			7DoF 2nd order analysis for LTB	

Then introduce a beam nonlinearity on your member.



Two extra types are now available:

- Members with Initial Stress;
- Cable Elements.

5.2.1 Members with Initial Stress

Tensile forces in elements augment the stiffness of the structure. Compression forces reduce the stiffness. Adding initial stresses into the structure can therefore influence the stiffnesses and resulting deformations greatly. They are especially useful for cables, which will be looked at in the next part.

Initial stress in SCIA is regarded as follows:

- The element in question is taken from the structure.
- The initial stress is put on the element through the defined axial force.
- The element is put back into the structure.

It is clear that when the element is inserted into the structure, the initial stress will partly be given to other members thus the inputted force will not stay entirely in the member in question. This is why the internal forces in the results will be different from the inputted starting values.

Notes:

- A positive axial force signifies a tensile force; a negative axial force signifies a compression force.
- Initial Stress is mostly used in conjunction with a 2nd Order analysis.

There are two ways to enter initial stresses into a model. The first why is by adding the nonlinear data 'initial stress' or a cable with initial stress values into the model, and then choosing for the option **Stress from member nonlinear data** in the **solver setup**, together with **Initial stress**.

The second option is the **Stress from load case** option. Here you can select a load case and the internal forces caused by this load case will be used as the initial state for the calculation.

Initial stresses (both from load case or member data) are also used for the modal analysis, making it possible to introduce some part of nonlinear behavior in dynamic analysis. This is very useful to account for 2nd order and pre-tensioning effects on cables.

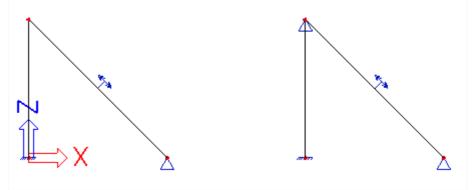
	Solver setup			×
	Name Specify load cases for linear calculation Specify combinations for nonlinear calculation			
	Advanced solver settings			
⊳	General			
Þ	Nonlinearity			
	Initial stress			1
	Initial stress	V		
	Stress from member nonlinearity data			L
	Stress from load case	p1	×	
Þ	Soil			
		ОК	Cancel	١.,

In theory, when using correctly defined values of the cross-section properties (surface A, moment of inertia I, modulus of Young E), a beam nonlinearity with Initial Stress can also be used to model straight cables with large pre-stress forces. Both **Timoshenko** and **Newton-Raphson** methods can be applied in this case.

In general however, for cables the use of the specific **cable element** is advised in conjunction with the **Newton-Raphson** method.

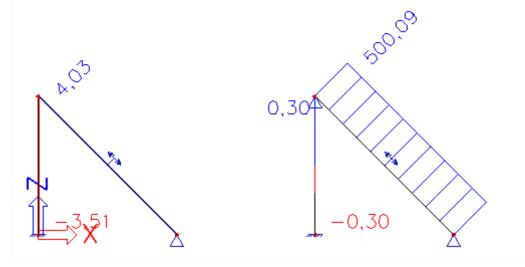
Example: Initial_Stress.esa

In this project, a simple frame is modelled. The diagonal has a RD30 section and is given an Initial Stress by means of a **tensile force** of **500 kN**.



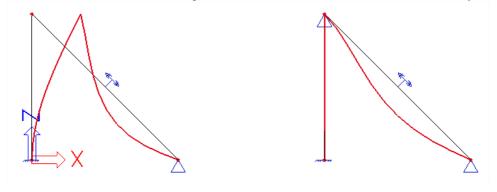
In the left frame, the initial stress will immediately be distributed to the column. In the right frame, the extra support will prohibit this.

A nonlinear analysis, taking into account the initial stress gives the following results for the normal forces:



As specified, in the left frame, the initial stress is immediately distributed to the rest of the structure so the tensile force of 500 kN is not found entirely in the diagonal. In the right frame, the force cannot be distributed due to the support so the 500 kN stays in the diagonal.

This principle is even more clear when looking at the deformed mesh for the nonlinear analysis:



5.2.2 Cable Elements – Not available in the Professional edition

Since SCIA Engineer version 21.1, cables are fully supported in the 64bit version in the default postprocessing environment. For cable analysis the module sens.03 is necessary. This module is included in the Expert and Ultimate edition.

A cable element is an element without bending stiffness (Iy and Iz \cong 0). During the solving of the equations this behavior is taken into account, so only axial forces (in tension only) will occur and you will obtain zero values for the internal forces M_x, M_y, M_z, V_y and V_z. The displacements (in the intermediate nodes) have thus been calculated without bending stiffness.

The cable type is a special type of a beam nonlinearity, which can be applied on 1D members in a model. You will need to create nonlinear combinations to take into account this nonlinear property during the analysis. A geometrical nonlinear analysis should be executed by calculating with a 3rd order analysis with the Newton-Raphson calculation method.

Theoretical background

A curve formed by a hanging cable is called a "Catenary". With relatively small bending (height - sag roughly 10% of its length) the curve can be approximated by a parabola (this approach was implemented previously in the 32bit version of SCIA Engineer in the post-processing environment 'v16 and older'), but such approximation however becomes imprecise with greater sag / length ratio (and for different heights of the begin and end nodes of the cable).

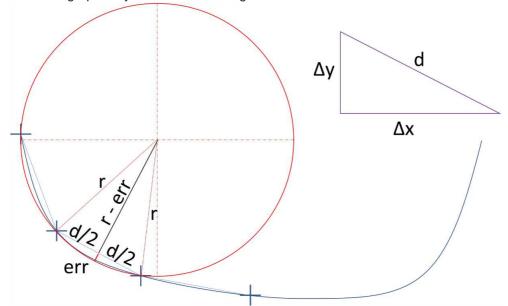
The catenary curve is linearly approximated into a polyline. The approximation points (nodes) are calculated from the catenary equation defined by two edge points of the beam and its parameter a, which is defined as a quotient (normal force / cable weight per unit length). The normal force is defined via the nonlinearity parameters and the cable weight per unit length is calculated from the cross-section and material parameters. Formula of the general catenary equation:

$$y = a \cdot \cosh\left(\frac{x - k}{a}\right) + c$$

Parameters k and c represent the horizontal and vertical shifts of the curve, respectively. The relation between catenary length s, vertical span of two definition points v and their horizontal span H is:

$$\sqrt{s^2 - v^2} = 2 \cdot a \cdot \sinh\left(\frac{H}{2a}\right)$$

You have full control of the catenary curve approximation precision. A general curvature approach has been utilized. Using the curvature (parameter defining how much the curve bends at the given point) the radius of the circles (of the same curvature as the curve in the touching point) is calculated. Concept of the approximation error is graphically described in the figure below:



The detailed background (including formula to calculate the value of sag) can be found on our help-pages: https://help.scia.net/webhelplatest/en/#analysis/nonlinear_analysis/cables/cable.htm

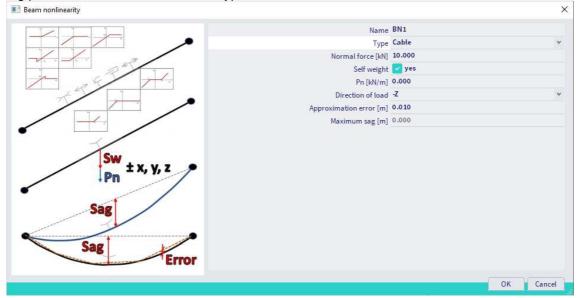
Modelling

In order to apply the cable nonlinearity to 1D elements, the functionalities Nonlinearity and Cables should be turned on in the Functionality tab of the Project settings dialog. When the Cables functionality is turned on, automatically the functionality Geometrical nonlinearity is turned on as well.

You can assign the nonlinearity 1D for a 1D member via Input Panel > workstation Structure > category Boundary conditions > Nonlinearity 1D:

Ξ	INPUT PANEL
	Structure \checkmark
-	Boundary conditions $$
0	All tags 🗸
NONL	INEARITY 10 🗟 📥 👗 🤗 📂 🎁 🕂
*	≝ œ œ œ

Following parameters are available for the type cable:



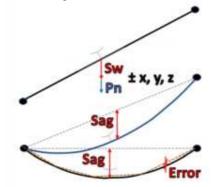
- Normal force [kN]:
- Self-weight:
- Pn [kN/m]: •
- Direction of load:
- Maximum sag [m]

value of the pre-stressing axial force (positive)

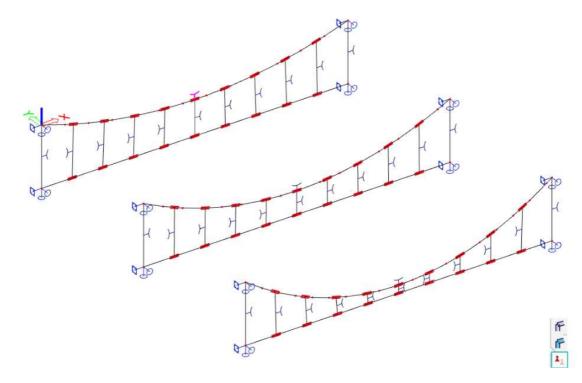
determines, whether the cable is subjected to self-weight

specifies the value of the additional load (so other than self-weight)

- specifies the load direction (Pn and self-weight)
- Approximation error [m]: determines the maximal allowed distance between point on the analytically defined catenary curve and the projection of this point (in the direction of load) on the linearly approximated polyline of the cable.
 - automatically calculated value, it is the maximal distance (in the direction of load) between a node of the catenary curve and its projection on the straight line connecting both ends of the cable



Alternation of these parameters automatically causes the geometry change of the catenary curve. The geometry is also automatically altered after the coordinate change of the begin or the end node of the cable. If there are more cables attached to each other, e.g. through the internal nodes, these mutual connections are preserved after the geometry alternation of the cable member and the relative positions of the internal nodes within the cable length remain the same.



Analysis

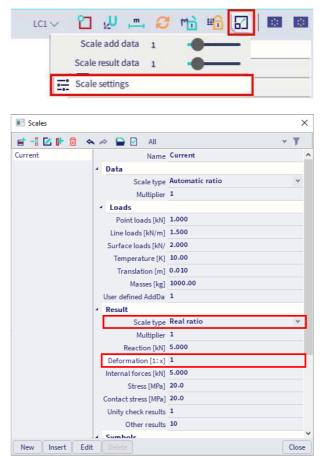
The average number of 1D mesh elements on straight 1D members (linear approximation between the nodes of the catenary curve) needs to be at least 4 (in the mesh setup).

A nonlinear combination needs to be defined, and the geometrically nonlinear analysis calculated. Large deformations needs to be considered (3rd order), along with the Newton-Raphson method of calculation (to be defined in the solver setup). If there are problems with convergence, increase the values of *Number of increments*, or *Maximum iterations*. Additionally, the *Solver precision ratio* or *Solver robustness ratio* might be altered to have an influence on the convergence criteria as well.

📧 FE analysis		>			
Calculations	Mesh setup				
	Average number of 1D mesh elements on straight 1 4				
Linear analysis Load cases: 1 Nonlinear analysis Nonlinear combinations; 1	Average size of 1D mesh element on curved 1D mer 0.200				
	Average size of 2D mesh element [m] 1.000				
	Connect members/nodes 🗹				
	Setup for connection of structural entities				
)ther processes	Advanced mesh settings				
Test input of data	✓ Solver setup				
Save project after analysis	Specify load cases for linear calculation Specify combinations for nonlinear calculation				
	Advanced solver settings				
	▷ General				
	A Nonlinearity				
	Geometrical nonlinearity 3rd order (large deformation)	*			
	Method of calculation Newton-Raphson	*			
	Number of increments 5				
	Maximum iterations 20				
	Solver precision ratio 1				
	Solver robustness ratio 1				
	Initial stress				
[Stability				
Calculate	▲ Soil				

Results

In order to see the real scale of the results (the default scale is exaggerated artificially since the biggest value is scaled to 1 m), it is necessary to set the real ratio and the multiplier equal to 1 within the Scale settings:

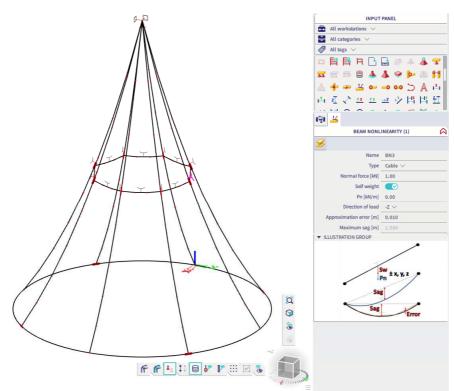


Notes:

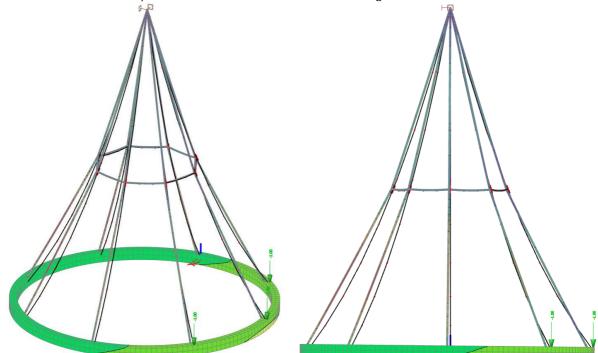
- The input of the cable element only defines the initial shape / sag. Afterwards the cable can be loaded by real loads. The normal force after calculation will therefore be different to the inputted initial normal force N.
- Adding a cable into the model will adapt the mesh also for the linear calculations. This means that the linear calculation may become unstable when a cable is added, and a nonlinear calculation becomes necessary to obtain results.

Example: Chandelier.esa

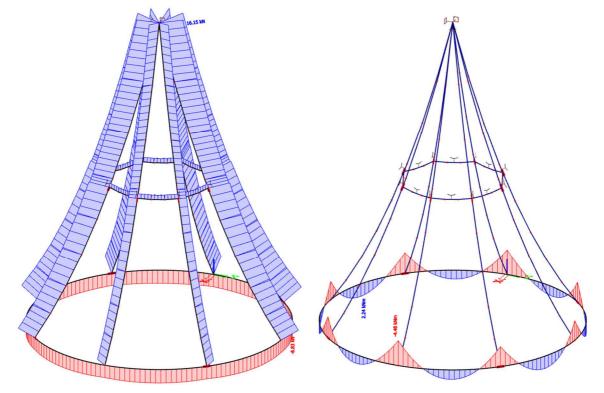
To illustrate the application of cables, a chandelier is modelled. A circular ring hangs with cables to one support at the top. These cables have a normal force of 1 kN and self-weight activated. The cables are also connected with each other by other cables with the same properties.



We consider a nonlinear combination NC1 which contains the self-weight of the structure and three points loads of 1 kN. In the 3D displacements we notice that the load straightens the curved elements:

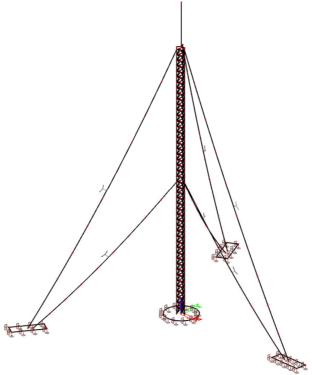


In the cables, the only non-zero values of internal forces are for the normal forces N (tension). On the right picture we can see that there are no bending forces present in the cables:

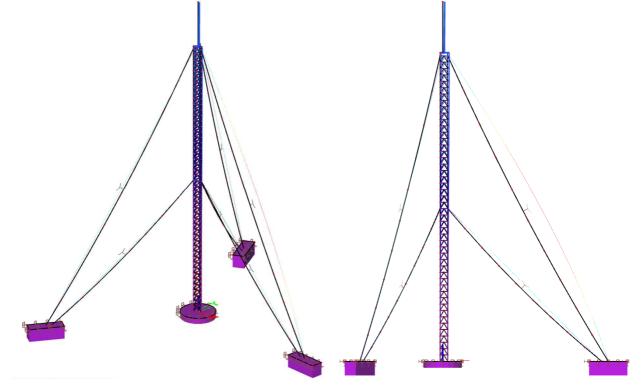


Example: Spire.esa

Another application of cables is a spire. The mast is supported by several cables which have a prestress force of 5 kN and self-weight activated.



The 3D displacement for nonlinear combination NC1 (which includes a horizontal wind load) for example shows the following:



N

5.3. Nonlinear Member Connections

When inputting hinges on beam elements, it is possible to input a nonlinear function for each degree of freedom (**ux**, **uy**, **uz**, **fix**, **fiy**, **fiz**). The function can signify the relation between moment and rotation or force and displacement.

📑 Hinge on beam			
	Name	H38	
¢Ζ	Position	Begin	
Ť	ux	Rigid	2
	uy	Rigid	
	uz	Rigid	
ux uy	fix	Rigid	
φχ	fiy	Nonlinear	
	Stiff - fiy [kNm/mrad]	3,9149e+01	
	Fun - fiy	Node : N2-[B3]	×
	fiz	Rigid	
			OK Cancel

When using nonlinear functions, it is very important to input a relevant linear stiffness. This value is used for the linear calculation, and during the first iteration of the nonlinear calculation.

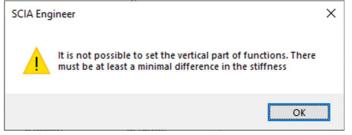
Nonlinear functions

The nonlinear functions can be entered in this menu:

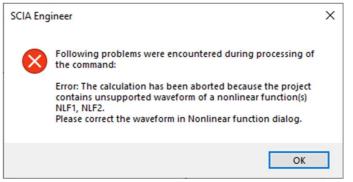
		12	Nonlin	ear functi	ons	_		
[Nonlinear funct	ions						×
	🎜 🦆 🏒 📸 👢	<u>n</u> a	8	ê 🖻 🗧	All			¥ (7
Ĩ	lode : N2-[B3]							
						203.59 135.59		
		Node: N2	·[B3]	-				
		Rotation		-23.3120		1.1700 0000 0000 0000 0000 0000 0000 000		
	Positive end		*	<u>- 8</u>		0.00		
	Negative end	Free	*	1		8161. 7017.	23.3120	fi [mrad]
1	Impulse	22.2420.4	202.50				8	
	1 [mrad,kNm]							
	2 [mrad,kNm]					-135.59		
	3 [mrad,kNm]							
	4 [mrad,kNm]					-203.59		
	5 [mrad,kNm]							
	6 [mrad,kNm]					'		
	7 [mrad,kNm]	23,3120 / 2	03,59					
	Create new function	New	Insert	Edit				Close

For member connections, the nonlinear functions can be defined for translation or rotation. When defining a function, it is very important to check the signs of the function values. The defining magnitudes for nonlinear rotation functions are the internal forces, for nonlinear translation functions the displacements. This implies that these functions are inputted in the first and third quadrant.

One must also make sure that the function does not contain any vertical parts, as this would lead to problems in the calculation with multiple possible solutions for one value. When entering a vertical part, the following message will be displayed:



In older versions of SCIA engineer it was possible to introduce vertical parts. Therefore, when opening an old project, it is possible that it contains such a function. In this case an error message will appear when running the calculation:



For the end of the function, it is possible to select one of three options:

- Free: When the maximal force is reached, it stays at that value and the deformation will rise uncontrolled.
- Fixed: When the maximal deformation is reached, it stays at that value and the force component will rise.
- Flexible: The relation between force component and deformation is linear.

SCIA Engineer also allows creating a new function from the already defined functions to provide an easy input of complex functions.

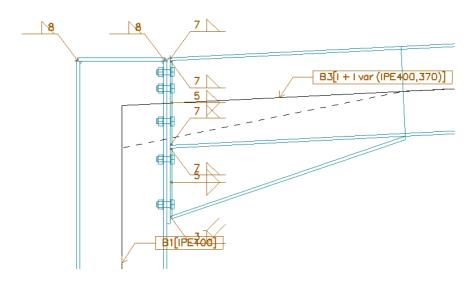
Example: Connection.esa

In this example, an industrial hall is calculated using algorithms to calculate the moment-rotation diagram for bolted and welded beam-to-column connections. SCIA Engineer allows the calculation of these diagrams and the automatic application of the diagram as a nonlinear spring function for member connections. For the theoretical background, reference is made to the "Advanced Training Steel" and ref. [13].

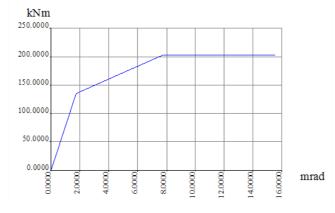
The geometry of the structure is shown in the following figure:

The structure is calculated in 2nd Order using **Timoshenko's** Method. The diagonals have been set as **Tension-only**.

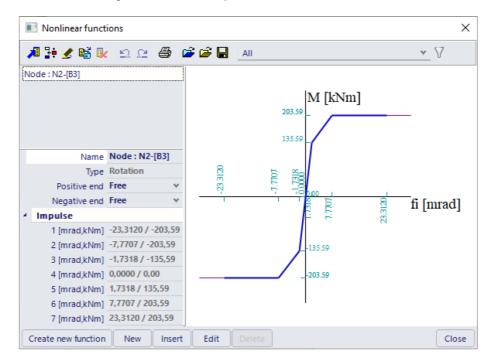
In node N2 a bolted beam-to-column connection is modelled:



The Moment-Rotation diagram is calculated by SCIA Engineer using the algorithm of the EN 1993-1-8.



Together with the calculated diagram, automatically a nonlinear function is created:



The function characterizes both tension-on-top and tension-at-bottom.

This function can then be assigned to the hinge defined in node N2:

Name	H37		
Position	Begin \checkmark		
ux	Rigid \checkmark		
uy	Rigid 🗸		
uz	Rigid \sim		
fix	Rigid 🗸		
fiy	Nonlinear \checkmark		
Stiff - fiy [kNm/mrad]	39,15		
Fun - fiy	Node : N2-[B3] ∨		
fiz	Rigid \lor		
Member	83		

5.4. Support Nonlinearity

SCIA Engineer allows the following types of nonlinear supports:

- Tension only / Pressure only supports;
- Nonlinear springs for supports;
- Friction supports.

5.4.1. Tension only / Pressure only Supports

To input nonlinearities for supports, the functionality **Nonlinearity > Support nonlinearity/basic soil spring** must be activated.

	GENERAL	D	ETAILED	
	Property modifiers		Nonlinearity	
	Model modifiers		Beam local nonlinearity	
	Parametric input		Support nonlinearity/basic soil spring	
	Climatic loads		Initial imperfections	
-	Mobile loads		Geometrical nonlinearity	
	Dynamics		General plasticity	
	Stability		Cables	
	Nonlinearity 🗹		Friction support/Soil spring	
	Structural model		Subsoil	
E	IFC properties		Pad foundation check	
	Prestressing		Steel	
E	Bridge design		Plastic hinge analysis	
Enter	Excel checks		Fire resistance checks	
	Substitution beam		Steel connections	
-			Scaffolding	
E			7DoF 2nd order analysis for LTB	
An other Same			Girders with sinusoidal webs	

Supports with tension can be automatically eliminated. This is mostly used for slabs on subsoil, column bases of for example scaffoldings, struts, ...

The following types of supports can be eliminated if tension occurs:

- Nodal Support;
- Line Support;
- Subsoil.

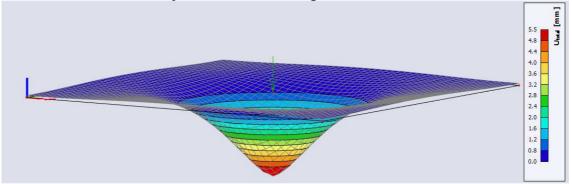
For nodal supports or line supports it is possible to specify a translation degree of freedom as **Rigid pressure only** or **Flexible pressure only**.

Subsoils are always regarded as **pressure only** for a nonlinear calculation, if the functionality **Support nonlinearity/Soil spring** is ticked on.

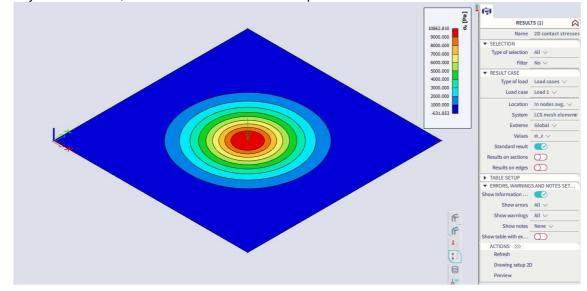
Support in node		×
Support in node	Angle [deg] Constraint X Z	Sn3 Standard v Custom v Free v Free A Free A Rigid Fiexible Rigid press only Rigid press only
		OK Cancel

Example: Subsoil.esa

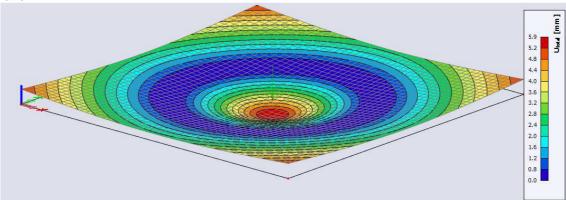
In this example, a slab on subsoil is calculated. The slab is loaded by a point force in the middle. The deformation for the **linear analysis** shows the following:



Especially in the corners, tensile contact stresses are expected:



A **nonlinear analysis**, taking into account the pressure-only characteristic of the subsoil shows the following deformation:



4000.000 3000.000 2000.000 1000.000 0.000

As can be seen, the slab will rise at the corners so no more tensile contact stresses are obtained:

The pressure stresses in the middle have increased which is expected when the slab can rise at the corners.

Notes:

- When using subsoil, it is important to adequately refine the mesh in order to produce precise results.
- When calculating following the Winkler theory, the Pasternak values (C2) must be set to zero.

5.4.2 Nonlinear Springs for Supports

As seen for nonlinear member connections, it is also possible to use nonlinear functions for supports. For each degree of freedom (X, Y, Z, Rx, Ry, Rz) a nonlinear function can be inputted. The function can signify the relation between moment and rotation or force and displacement.

Support in node			×
	Name	Sn3	
	Туре	Standard	¥
	Angle [deg]		
	Constraint	Custom	¥
	х	Free	Y
	Z	Nonlinear	¥
AZ /	Stiffness Z [N/mm]	6,2800e+02	
	Function Z	NLF1	×
X Ry	Ry	Free	٧
	Default size [m]	0,200	
(i)	Geometry		
\smile	System	GCS	۷
$\hat{\mathbf{r}}$			
			OK Cancel

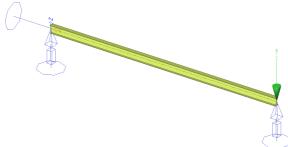
When using nonlinear functions, it is very important to input a relevant linear stiffness. This value is used during the first iteration of the nonlinear calculation (and during a linear calculation).

The definition of the nonlinear functions is exactly the same as seen with nonlinear member connections.

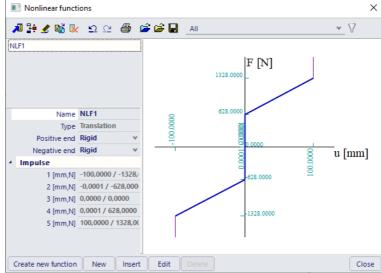
In addition to nodal supports, a nonlinear function can also be used for a subsoil under a plate.

Example: Support_Function.esa

In this example, the use of a nonlinear function for a support is illustrated. A simple beam on two supports is modelled.



The **translation Z** of both supports has been defined as a nonlinear function:



The beam is loaded by a point force at one end. The value of the point force is taken as 1kN and 1.4kN.

A nonlinear analysis shows the following deformation for the load of 1kN:



This value can manually be approximated as follows:

$$U_{z} = \frac{-100 \text{ mm}}{-1328 \text{ N} + 628 \text{ N}} \cdot (-1000 \text{ N} + 628 \text{ N}) = -53,14 \text{ mm}$$

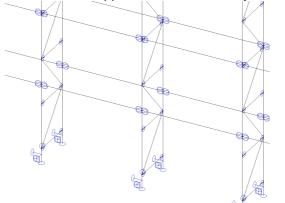
For the load of **1.4 kN**, the fixed end of the function is reached thus the maximal deformation of 100 mm is obtained:



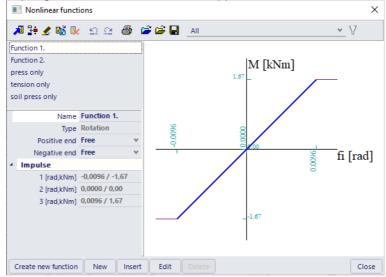
Example: Pallet_Racking.esa

In this example, the calculation of a pallet racking system is shown according to ref. [9] Eurocode ENV 1993-1-1 and ref. [10] FEM 10.0.02. This last reference gives field test methods which allow the definition of moment-rotation diagrams for beam-to-column connections and column supports.

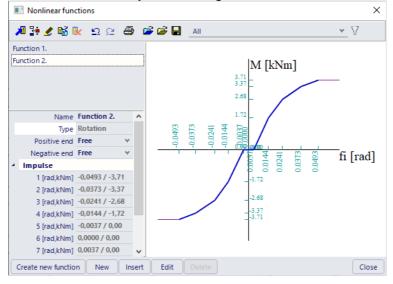
The beam-to-column connections and column supports can be defined by means of nonlinear functions.



The following nonlinear spring is defined for the column supports:

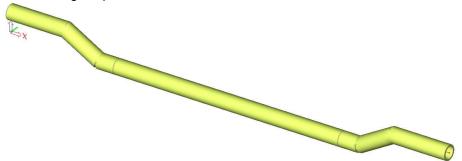


The beam-to-column connections are defined by the following nonlinear characteristic:

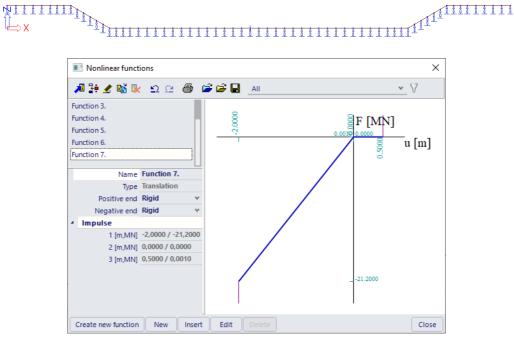


Example: Culvert.esa

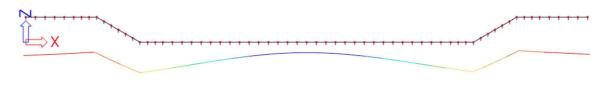
This project illustrates the use of nonlinear functions to model for example the soil under a culvert. The culvert has the following shape:



Nonlinear supports have been defined with appropriate functions to model the behaviour of the soil:



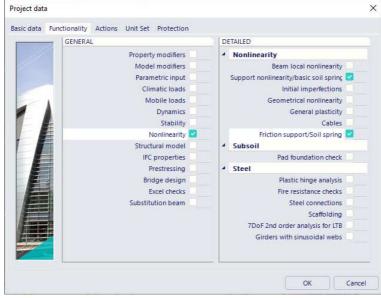
A nonlinear analysis gives the following deformation pattern for combination NC2:



5.4.3 Friction Supports

Friction supports can be used to model the fact that a reaction component is dependent on another component. The horizontal component is for example dependent on the vertical component. When the friction force is surpassed, the support slips through resulting in large deformations.

To input friction supports, both the functionalities **Nonlinearity > Support nonlinearity/Basic soil spring** and **Friction support/Soil spring** must be activated.



When entering a nodal support, the option **Friction** can be chosen for the translational degrees of freedom (**X**, **Y**, **Z**).

Support in node					\times
	Name	Sn28			^
	Type	Standard		~	
2	Angle [deg]				
^{Rz}	Constraint	Custom		~	
Z	X	Friction		Y	
Y	From reaction	Y		^	
Rx	C flex X [kN/m]	Y		h	
i	mju X	Z YZ			
	Y	Y+Z			
Z	Z	Rigid		~	
	Rx	Free		v	
X	Ry	Free		~	
	Rz	Free		۷	
	D . f 14 F1	0 200			~
			ОК	Cance	el

The option From Reaction is used to specify which force component causes the friction force.

X, Y, Z: The final limit force can be calculated from the reaction in a specified direction. If a support in the X-direction is being defined, it can be said that the friction force should be determined from the reaction calculated in either the Y or Z direction. The friction force is calculated from the following formula:

 $mju \cdot R_{r}$

XY, XZ, YZ: The final limit force can be calculated as a compound friction. Only one of the stated options is offered for each direction. E.g. if a support in the X-direction is being defined, it can be said that the friction force should be determined from the reactions calculated in the Y and Z direction. The friction force is calculated from the following formula:

$$mju_x \cdot \sqrt{R_y^2 + R_z^2}$$

X+Y, X+Z, Y+Z: The same as above applies here. A different procedure is however used to calculate the limit force. E.g. for a friction support in the X-direction the following formula is employed:

$$mju_x \cdot R_y + mju_x \cdot R_z$$

In these formulas, mju specifies the coefficient of friction.

In the field **C flex**, the stiffness of the support can be inputted.

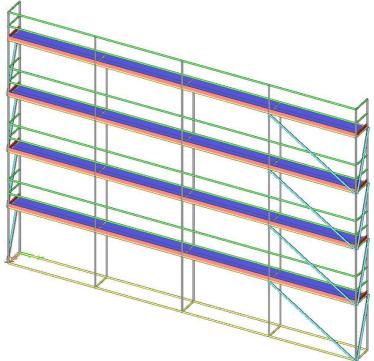
Notes:

- Friction can be inputted in one or two directions. It is not possible to define friction in all three directions since otherwise the "thrust" cannot be determined.
- When simple friction (X, Y, Z) is defined in two directions, the option Independent is available. This specifies that the friction in one direction is independent on the friction in the other direction.
- Composed friction (e.g. YZ or Y+Z) can be specified only in one direction.

Friction supports can be used for several types of structures. Nearly every support which isn't rigidly connected to the surface on which it stands is subjected to friction. Examples include base jacks of scaffolding structures, supports on an inclined surface, pipes in boreholes,...

Example: Scaffolding.esa

This project illustrates the use of friction supports for a scaffolding structure. The scaffold has the following geometry:

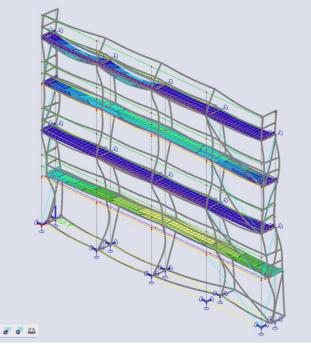


The base jacks are inputted as friction supports. Since a base jack, by default, is not connected to the surface, the Z-direction is defined as rigid **Pressure-only**. Both horizontal degrees of freedom X and Y are defined as **Friction**, dependent on the reaction Z.

SUPPORT	IN NODE (1)	5
SUPPORT		
Name	Sn9	
Туре	Standard \checkmark	
Angle [deg]		
Constraint	Custom	\sim
Х	Friction \lor	
From reaction	Ζ 🗸	
C flex X [kN/m]	1000,00	
mju X	0,20	
Y	Friction \checkmark	
From reaction	Z 🗸	
C flex Y [kN/m]	1000,00	
nju Y	0,20	
Z	Rigid press only \smallsetminus	
Independent friction	\bigcirc	
Rx	Free V	
Ry	Free 🗸	
Rz	Free 🗸	
Default size [m]	0,20	
	N17	
 GEOMETRY System 	GCS 🗸	

When large wind loads are taken into account, for example due to netting, large horizontal reaction forces are expected in the base jacks. When these reactions surpass the friction force, the support slips through.

After a **nonlinear analysis** of the scaffold, the **deformed mesh** for combination **NC4** shows the following:



In the middle base jacks, the friction force is clearly surpassed and thus the supports slip through. To avoid this, the reaction in Z-direction must be augmented thus extra dead weight like ballast will be required or the base jacks must be fixed to avoid slipping.

<u>Note:</u> the functionality **Nonlinear Line Support** defines a specific type of soil spring developed for the Pipfas project (Buried Pipe Design).

5.5 2D Elements

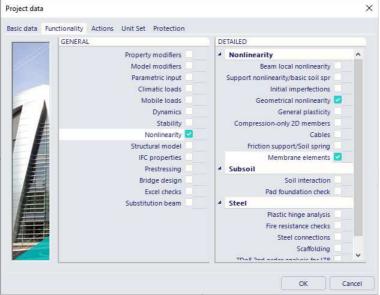
5.5.1 2D Membrane Elements – Not in Professional Edition

This option is implemented in module sens.03 and included in the Expert edition. So with the Professional edition the option of Membrane elements as described in this chapter, will not be possible.

Membrane elements are defined as shell elements which have no flexural stiffness and no axial compression stiffness. Membrane elements can thus be used to model canvas, nets, etc. that are subjected to axial tension.

To obtain realistic results, a 2nd order calculation needs to be executed using the Newton-Raphson method.

To input 2D membrane elements, the functionalities **Nonlinearity > Geometrical nonlinearity** and **Membrane Elements** must be activated.



When defining the 2D element, the option Membrane must be chosen as FEM nonlinear model.

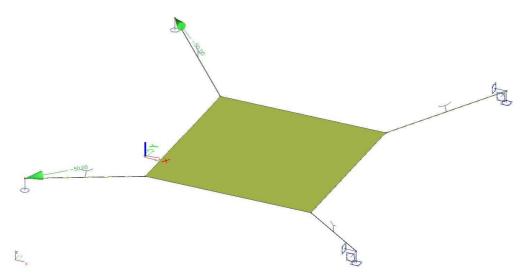
2D member					×
	Name	S2			
	Element type	Standard			¥
	Element behaviour	Standard FEM			
	Туре	plate (111)			۷
Μ5α	Material	Textile		~	
τ	FEM model	Isotropic			٧
	FEM nonlinear model	Membrane			٨
	Thickness type	none			
ez	Thickness [mm]	2 Z	2		
/	LCS type	Standard			۷
	Swap orientation	no			
	LCS angle [deg]	0,00			
IZ	Layer	Layer1		~	
2					
x y					
			ОК	Cance	

Notes:

- Membrane elements can only be modelled in a General XYZ environment.
- Due to the fact the flexural rigidity is zero, no ribs, orthotropic parameters or physical nonlinear data can be inputted on a membrane element.
- Since a membrane element has no axial compression stiffness, no concrete calculation can be performed on this type of element.

Example: Membrane.esa

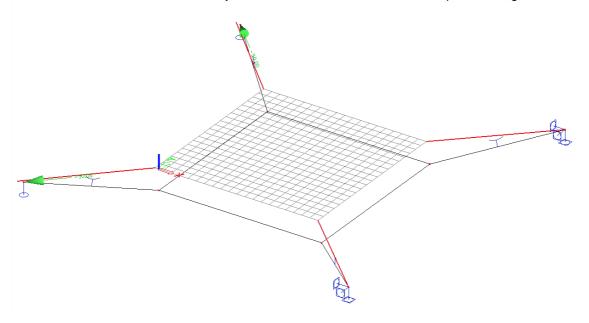
For this example, the 32bit version of SCIA Engineer is needed. In this project, a textile canvas is modelled. At the four corners of the canvas, steel cables are attached. Two cables are subjected to a tensile force of **50kN** in horizontal direction.



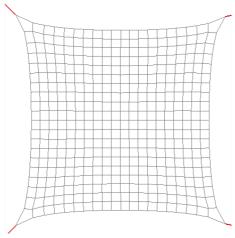
Since the canvas has an initial position **0,5m** lower than the endpoint of the cables, the canvas will first be pulled straight.

Since both cable and membrane elements are used, a 3rd order nonlinear analysis is executed using the Newton-Raphson method.

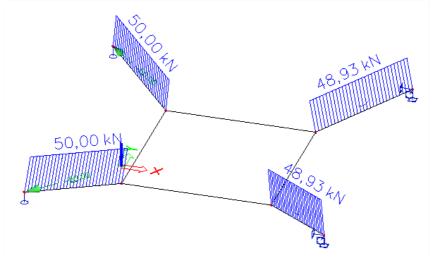
The deformed mesh for the nonlinear analysis shows that the canvas has been pulled straight:



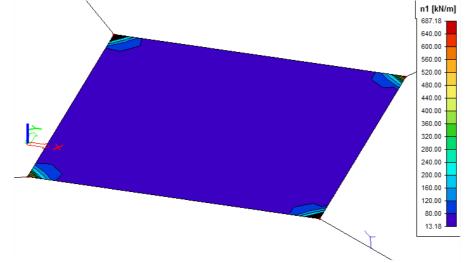
When the scale of the results is augmented, the typical deformation of the membrane element can clearly be seen:

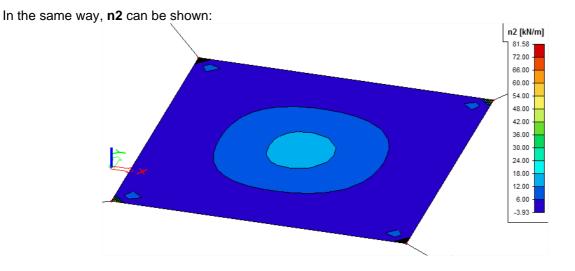


The tensile forces for the cable elements are shown on the following figure:



The principal membrane force n1 shows the tensile forces in the canvas:

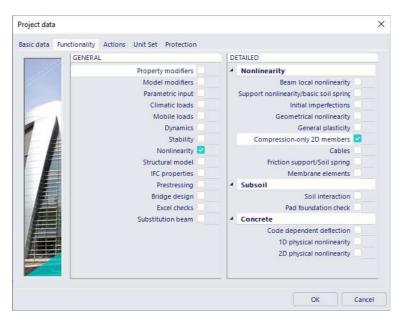




The results show the 2nd order effect: due to the tensile forces in one direction, the canvas obtains a stiffness which results in compression membrane forces.

5.5.2. Pressure only

To input pressure only for 2D elements, the functionality **Nonlinearity** and **Compression - only 2D members** must be activated.

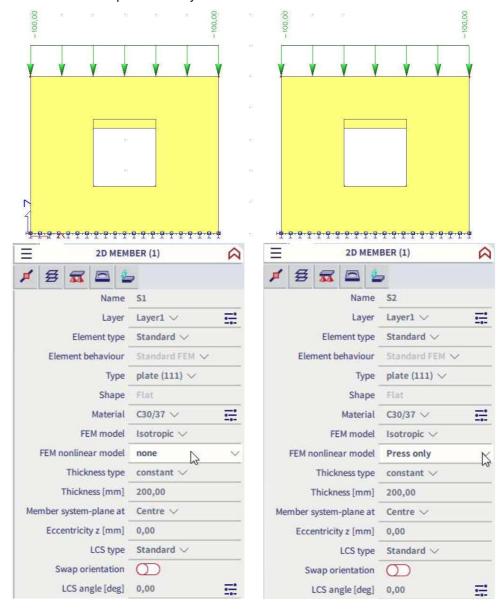


With this option, tension in 2D elements can be automatically eliminated. This is mostly used for masonry elements.

Example: PressureOnly.esa

This project illustrates the use of pressure only elements.

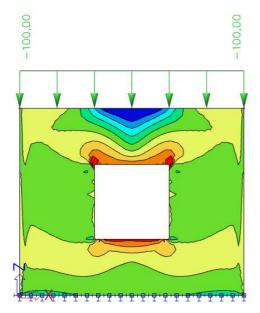
In this project two 2D-elements are modelled. The first one is modelled as an isotropic element with no nonlinearity, the second one is a pressure only element:

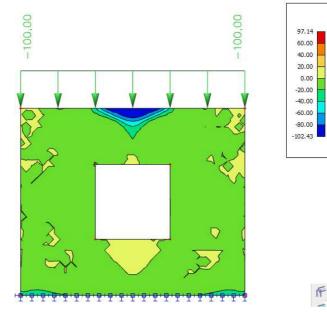


When calculating those elements, for every mesh element a certain orthotropy will be inserted. At the first iteration step all the pressure only elements, will be calculated as an isotropic element. After the first calculation, SCIA Engineer will input another stiffness on all elements in tension. So a certain orthotropy will be created. With this stiffness the tension capacity of this element will decrease. After adapting the orthotropic parameters a new calculation will be performed. After this second iteration step again the elements in tension will get another stiffness. This process will be repeated until equilibrium is reached.

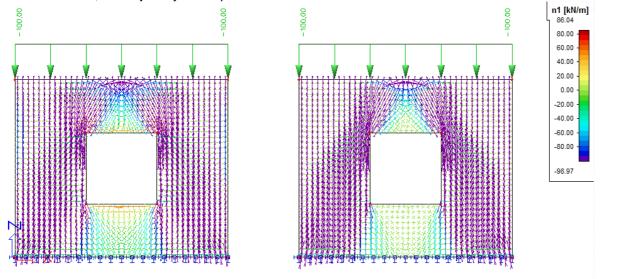
nı [kNm]

The difference between the isotropic and orthotropic elements can be clearly view looking at the principal normal force n1 for these members:





In these results the real pressure of this element is visible for the right element. Looking at the trajectories of this normal force, the trajectory of the pressure force will be even more visible:



Physical Nonlinearity

When the stresses are dependent on the strains in a nonlinear way, the nonlinearity is called a physical nonlinearity.

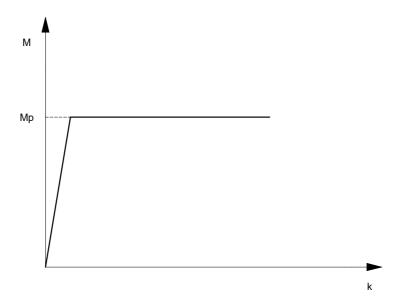
In SCIA Engineer, the following types of physical nonlinearities have been implemented:

- **Plastic hinges** for Steel Structures
- Physical nonlinear analysis for Concrete Structures
- General plastic analysis for 2D elements

6.1 Plastic Hinges for Steel Structures

This functionality handles the plastic behaviour of 1D elements. When a normal linear calculation is performed and limit stress is achieved in any part of the structure, the dimension of critical elements must be increased. If however, plastic hinges are taken into account, the achievement of limit stress causes the formation of plastic hinges at appropriate joints and the calculation can continue with another iteration step. The stress is redistributed to other parts of the structure and better utilization of overall load bearing capacity of the structure is obtained.

The material behaves linear elastic until the plastic limit is reached after which it behaves fully plastic. The σ - ϵ diagram thus has the same shape as the Moment-Curvature diagram:



The full plastic moment is given as M_p , the curvature as **k**.

In SCIA Engineer, a plastic moment can only occur in a **mesh node**. This implies that the mesh needs to be refined if a plastic hinge is expected to occur at another location than the member ends.

The reduction of the plastic moment has been implemented according to the following codes: **EC3**, **DIN 18800** and **NEN 6770**.

There is off course a risk when taking plastic hinges into account. If a hinge is added to the structure, the statically indeterminateness is reduced. If other hinges are added, it may happen that the structure becomes a mechanism. This would lead to a collapse of the structure and the (nonlinear) calculation is stopped.

On the other hand, plastic hinges can be used to calculate the plastic reliability margin of the structure. The applied load can be increased little by little (e.g. by increasing the load case coefficients in a combination) until the structure collapses. This approach can be used to determine the maximum load multiple that the structure can sustain.

To take into account plastic hinges for steel structures, the functionality **Steel > Plastic Hinge analysis** must be activated._____

	GENERAL	D	ETAILED
	Property modifiers		Nonlinearity
	Model modifiers		Beam local nonlinearity
	Parametric input		Support nonlinearity/basic soil spring
	Climatic loads		Initial imperfections
1	Mobile loads		Geometrical nonlinearity
	Dynamics		General plasticity
	Stability		Cables
-	Nonlinearity 🗹		Friction support/Soil spring
	Structural model		Subsoil
	IFC properties		Pad foundation check
	Prestressing		Steel
	Bridge design		Plastic hinge analysis
	Excel checks		Fire resistance checks
	Substitution beam		Steel connections
			Scaffolding
			7DoF 2nd order analysis for LTB
1005			Girders with sinusoidal webs

The choice of code which needs to be applied can be specified through **Menu bar > Tools > Calculation & Mesh > Solver settings.** The no code option simply follows the EC-EN logic.

.	iolver setup			×
	Coefficient for reinforcement	1		^
	Print time in Calculation Protocol			
	Nonlinearity			
	Method of calculation	Picard	¥	
	Number of increments	1		
	Maximum iterations	50		
	Solver precision ratio	1		
	Solver robustness ratio			
	Plastic hinge code	EC	~	
	Initial stress	No code		
	Initial stress	EC	2	
	Soil	NEN	~	
	Soilin			
	Step for soil/water pressure [m]	0,500		
	Soil combination		*	
	Maximum soil interaction iterations	10		
	C1x [MN/m^3]	1,0000e-01		
	C1y [MN/m^3]	1,0000e-01		
	C1z [MN/m^3]	1,0000e+01		
	C2x [MN/m]	5,0000e+00		~
R		ОК	Cance	
				d

It is not possible to choose on what members or in which nodes plastic hinges can be formed. If the functionality is activated, a plastic hinge will form wherever the moment resistance is exceeded regardless of the element's plastic capacity.

Example: Plastic_Hinges.esa

In this project, a continuous beam is considered. The beam has a cross-section type IPE 300 and is fabricated in S235.

According to Eurocode 3, the plastic moment resistance around the y-axis is given by:

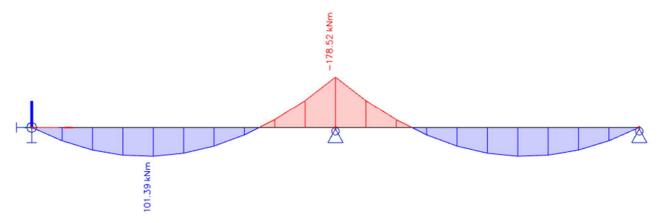
Axis system	Plastic bending moment resistance	Reduced plastic bending moment resistance for high normal force	Reduced plastic bending moment resistance for high shear force	Reduced plastic bending moment resistance for high normal force and high shear force
у-у	$M_{y,pl,Rd} = rac{W_{pl,y}*f_y}{\gamma_{M0}}$	$M_{y,N,Rd} = M_{y,pl,Rd} * rac{1-n}{1-0,5*a}$	$M_{y,V,Rd}=M_{y,pl,Rd}*~(1- ho_z)$	$M_{y,N,V,Rd}=M_{y,N,Rd}*~(1- ho_z)$
Z-Z	$M_{z,pl,Rd} = rac{W_{pl.z}*f_y}{\gamma_{M0}}$	$M_{z,N,Rd} = M_{z,pl,Rd} * \left[1 - \left(rac{n-a}{1-a} ight)^2 ight]$	$M_{z,V,Rd}=M_{z,pl,Rd}*~(1- ho_y)$	$\overline{M_{z,N,V,Rd}=M_{z,N,Rd}*~(1- ho_y)}$

For the beam (no normal or high shear force present) considered this gives the following:

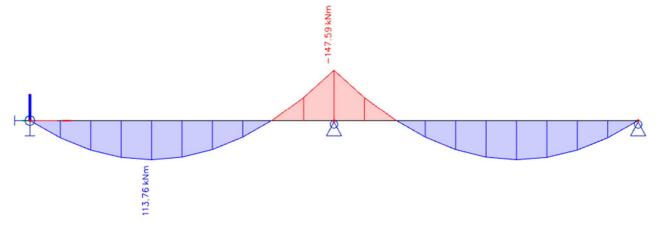
- $f_y = 235 \text{ N/mm}^2$
- W_{pl,y} = 6.28 105 mm³
- γ_{M0} = 1.0

$$\Rightarrow M_{\text{pl,y,d}} = \frac{W_{\text{pl,y}} \cdot f_{y}}{\gamma_{M0}} = 147,59 \text{ kNm}$$

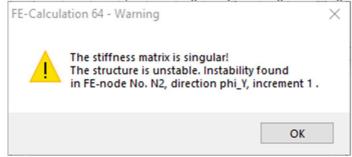
A **linear analysis** shows the following moment-diagram:



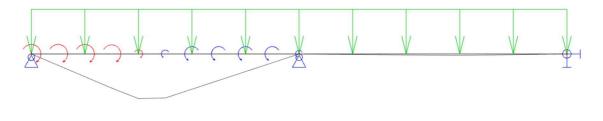
A nonlinear analysis taking into account plastic hinges gives the following result:



When the load is increased further, another plastic hinge will form in the middle of a span thus creating a mechanism. The nonlinear calculation will stop and a singularity message will be given:



The animation window shows the expected scene, where an additional plastic hinge in the middle of the span leads to a mechanism:



6.2 Physical Nonlinear analysis for Concrete Structures

This topic is regarded in detail in the course "Advanced Training Concrete".

6.3 General Plastic analysis

This functionality handles the plastic behaviour of any 2D members (plates, walls and shells). Four different criteria have been implemented to determine when the plastic behaviour is initiated: Von Mises, Tresca, Mohr-Coulomb and Drucker-Prager.

The plastic behaviour of materials may be combined with other types of nonlinearities in SCIA Engineer. It can be activated in the material setup, after selecting the right functionalities.

<u>Note:</u> general plasticity behaviour is not applied to 1D members. The 1D members that are present in the model will be considered as elastic.

6.3.1 Yield criteria

To determine whether the material should start behaving plastically, we first need to know if the yield strength has been reached. In SCIA Engineer, 4 different yield criteria have been implemented. Two for symmetrical, ductile materials (steel, aluminium,...): Tresca and Von Mises, and two for materials with different behaviour in compression and tension (concrete, masonry,...): Mohr-Coulomb and Drucker-Prager.

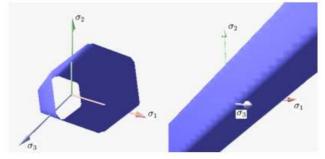
Tresca

The Tresca criterion is also known as the maximum shear stress theory (MSST) and the Tresca–Guest (TG) criterion. In terms of the principal stresses the Tresca criterion is expressed as:

$$rac{1}{2} ext{max}(|\sigma_1 - \sigma_2|, |\sigma_2 - \sigma_3|, |\sigma_3 - \sigma_1|) = S_{sy} = rac{1}{2}S_y$$

Where S_{sy} is the yield strength in shear, and S_y is the tensile yield strength.

On the picture below there is the Tresca–Guest yield surface in the three-dimensional space of principal stresses. It is a prism of six sides and having infinite length. This means that the material remains elastic when all three principal stresses are roughly equivalent (a hydrostatic pressure), no matter how much it is compressed or stretched. However, when one of the principal stresses becomes smaller (or larger) than the others the material is subject to shearing. In such situations, if the shear stress reaches the yield limit then the material enters the plastic domain.



Von Mises

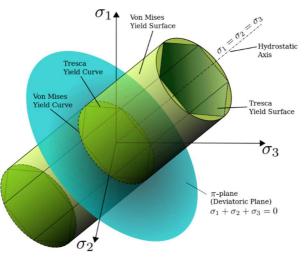
This criterion suggests that the yielding of materials begins when the second deviatoric stress invariant J2 reaches a critical value. For this reason, it is sometimes called the J2-plasticity or J2 flow theory. It is part of plasticity theory that applies best to ductile materials, such as metals. Prior to yield, material response is assumed to be elastic.

In materials science and engineering the von Mises yield criterion can be also formulated in terms of the von Mises stress or equivalent tensile stress, σ_E , a scalar stress value that can be computed from the Cauchy stress tensor. In this case, a material is said to start yielding when its von Mises stress reaches a critical value known as the yield strength, σ_y . The von Mises stress is used to predict yielding of materials under any loading condition from results of simple uniaxial tensile tests. The von Mises stress satisfies the property that two stress states with equal distortion energy have equal von Mises stress.

The Von Mises stress is expressed as:

$$\sigma_{\rm E} = \sqrt{\frac{1}{2} \cdot \left[(\sigma_{11} - \sigma_{22})^2 + (\sigma_{22} - \sigma_{33})^2 + (\sigma_{33} - \sigma_{11})^2 + 6 \cdot (\sigma_{12}^2 + \sigma_{23}^2 + \sigma_{31}^2) \right]}$$

Because the von Mises yield criterion is independent of the first stress invariant, I1, it is applicable for the analysis of plastic deformation for ductile materials such as metals, as the onset of yield for these materials does not depend on the hydrostatic component of the stress tensor, just like the Tresca criterion.



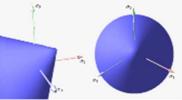
Drucker-Prager

The Drucker-Prager yield criterion is similar to the von Mises yield criterion, with provisions for handling materials with differing tensile and compressive yield strengths. This criterion is most often used for concrete where both normal and shear stresses can determine failure. The Drucker–Prager yield criterion may be expressed as:

$$\left(\frac{m-1}{2}\right)(\sigma_1 + \sigma_2 + \sigma_3) + \left(\frac{m+1}{2}\right)\sqrt{\frac{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}{2}} = S_{yc}$$

Where $m = \frac{S_{yc}}{S_{yt}}$ with S_{yc} and S_{yt} the uniaxial yield stresses in compression and tension respectively. If both are equal the formula reduces to von Mises.

The image shows the Drucker–Prager yield surface in the three-dimensional space of principal stresses. It is a regular cone.



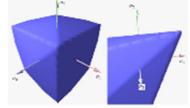
Mohr-Coulomb

The **Mohr-Coulomb yield** is similar to the Tresca criterion, with additional provisions for materials with different tensile and compressive yield strengths. This model is often used to model concrete, soil or granular materials. The Mohr–Coulomb yield criterion may be expressed as:

 $\frac{m+1}{2}\max(|\sigma_1 - \sigma_2| + K(\sigma_1 + \sigma_2), |\sigma_1 - \sigma_3| + K(\sigma_1 + \sigma_3), |\sigma_2 - \sigma_3| + K(\sigma_2 + \sigma_3)) = S_{yc}$ Where $m = \frac{S_{yc}}{S_{yt}}$ and $K = \frac{m-1}{m+1}$

The parameters S_{yc} and S_{yt} are the yield (failure) stresses of the material in uniaxial compression and tension, respectively. The formula reduces to the Tresca criterion if $S_{yc} = S_{yt}$.

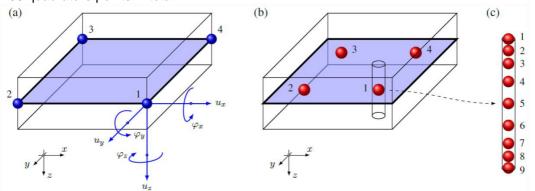
On the picture there is Mohr–Coulomb yield surface in the three-dimensional space of principal stresses. It is a conical prism and determines the inclination angle of conical surface.



6.3.2 Finite element model

Drilling rotations at each node is used for in-plane loading. This means that element has six degrees of freedom at each node and is therefore compatible with other types of elements (beam/solid elements).

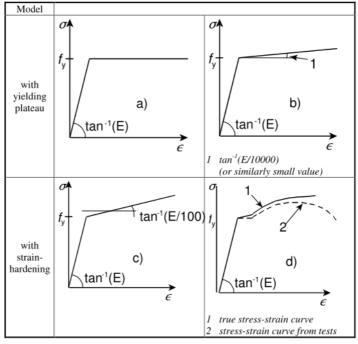
Within the element area the Gauss 2x2 quadrature points are used. Each of these Gauss quadrature points is realized by nine Gauss-Lobatto quadrature points throughout the thickness, so the four-node element has 2x2x9=36 quadrature points in total.



Due to these Gauss-Lobatto points the element can handle bending loading with high accuracy. In all of these points the nonlinear model is computed independently using the plane stress formulation. Linear transversal shear stiffness is assumed.

6.3.1 Material properties

Figure C.2 from EN 1993-1-5 is used for the material behaviour:



The different models are:

- a) elastic-plastic without strain hardening
- b) elastic-plastic with a nominal plateau slope
- c) elastic-plastic with linear strain hardening
- d) true stress-strain curve modified from the test results as follows: $\sigma = \sigma (1 + \varepsilon)$

$$O_{true} = O(1+\mathcal{E})$$

$$\mathcal{E}_{true} = \ell n \left(\mathbf{I} + \mathcal{E} \right)$$

In SCIA Engineer, a), b) and c) are implemented.

6.3.4 General plasticity in SCIA Engineer

General plasticity is a specific type of nonlinearity in SCIA Engineer. This means that **General plasticity** is a sub-functionality of the nonlinear analysis.

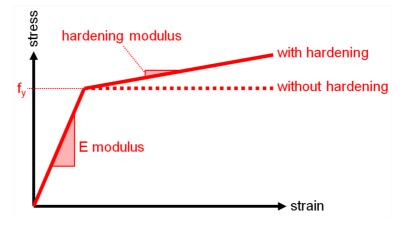
	GENERAL	DETAILED
11	Property modifiers	A Nonlinearity
	Model modifiers	Beam local nonlinearity
	Parametric input	Support nonlinearity/basic soil s
	Climatic loads	Initial imperfections
	Mobile loads	Geometrical nonlinearity
	Dynamics	General plasticity 🔽
	Stability	Compression-only 2D members
	Nonlinearity 🛃	Cables
	Structural model	Friction support/Soil spring
	IFC properties	Membrane elements
	Prestressing	✓ Subsoil
	Bridge design	Soil interaction
and the second second	Excel checks	Pad foundation check
	Substitution beam	▲ Steel
STRATES		Plastic hinge analysis
		Fire resistance checks

The nonlinearity of materials is defined directly in the material library. See the property group **Material behaviour for nonlinear analysis**.

Materia	ls		×
et -1 🗹	i 📅 🕪 💼 🐟 🗢 🛅 🔗 🖨 🖸 All	* Y	
S 235	Name	\$ 235	^
S 275	Code independent		
S 355	Material type	Steel	
	Thermal expansion [m/mK]	0,00	
	Unit mass [kg/m^3]	7850,0	
	E modulus [MPa]	2,1000e+05	
	Poisson coeff.	0,3	
	Independent G modulus		
	G modulus [MPa]	8,0769e+04	
	Log. decrement (non-uniform damping only)	0,15	
	Colour		
	Thermal expansion (for fire resistance) [m/mK]	0,00	
	Specific heat [J/gK]	6,0000e-01	
	Thermal conductivity [W/mK]	4,5000e+01	
	Price per unit [€/kg]	1,00	
	 Material behaviour for nonlinear analysis 		
	Material behaviour	Elastic	P
	* EC3	65	
	Ultimate strength [MPa]	360,0	
	Yield strength [MPa]	235,0	~
New 1	nsert Edit Delete	Close	se

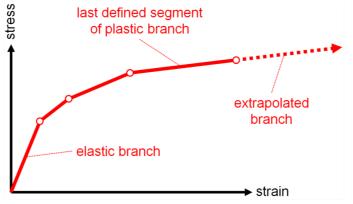
By default, all materials in the library are set as elastic. This means, that the selected material will behave elastically during a nonlinear analysis. The plastic properties of materials are generic, code independent in SCIA Engineer and are therefore available for any material, regardless of the selected design code.

Plasticity can be enabled by selecting a type of plastic behaviour. For steel, we can use **Isotropic elastoplastic von Mises**. It corresponds to a bilinear stress-strain relationship, identical in tension and compression. The plastic branch may have a slope (hardening modulus) or not. The stress-strain relationship is automatically generated from 3 parameters: Young's modulus (elastic part), yield stress for uniaxial tension and, optionally, hardening modulus (slope of the plastic branch).

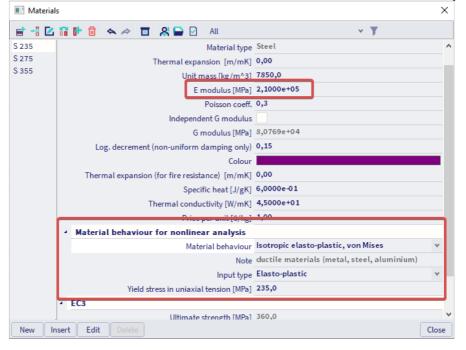


Only the tension part of the diagram is defined, as it is related to a plastification condition in general 3D stress state in principal stress directions. Some plastification models allow for a different yield stress in compression, which is defined separately. There is no limit (ultimate) strain value for the analysis.

When the actual strain value in the structure exceeds the defined diagram, the diagram is extrapolated, tangent to the last defined segment of the stress-strain relationship. The reason for that is, that the analysis would then fail and it would be impossible to find where the problem is located in the structure. It is therefore preferable, that the analysis continues and that you check the obtain strain values after the analysis.



The following parameters define the nonlinear behaviour of the material in the material library:



- **E modulus**: Young's modulus of the material which defines the slope of the elastic part of the stress-strain diagram
- Material behaviour: the type of material behaviour for the nonlinear analysis has to be selected
 - o Elastic
 - o Isotropic elasto-plastic, Tresca (ductile materials such as metal, steel, aluminium)
 - o Isotropic elasto-plastic, von Mises (ductile materials such as metal, steel, aluminium)
 - Isotropic elasto-plastic, Drucker-Prager (materials with difference in compressive en tensile strength such as concrete and soil)
 - Isotropic elasto-plastic, Mohr-Coulomb (materials with difference in compressive en tensile strength such as concrete and soil)
- **Input type: d**efines the definition of the plastic branch of the stress-strain diagram
 - *Elasto-plastic*: In the plastic domain, the stress remains constant when the strain increases
 - *Elasto-plastic with hardening*: In the plastic domain, the stress increases with the strain
- Yield strength: elastic limit for plastification due to shear
- Hardening modulus: slope of the plastic branch of the stress-strain diagram

<u>Note:</u> Various types of nonlinearity may be combined in the same project. However it is not possible to cumulate several types of nonlinearity on the same 2D member. The property *FEM nonlinear model* will behave as follows, when combined with a plastic material:

- Plastic material and 2D press-only behaviour: the press-only behaviour will be ignored and the 2D member will behave as plastic.
- Plastic material and membrane behaviour: the plastic behaviour will be ignored and the 2D member will behave as an elastic membrane element.

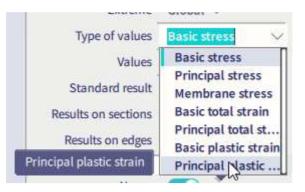
When starting the analysis, a warning message will be displayed giving the same information about functionality conflicts.

6.3.5 Checking strains

When using general plasticity, the stresses in the material will be topped off at the yield strength (or a bit higher if strain hardening is used). To check if the structure is stable, we will therefore need to check something different than the stresses.

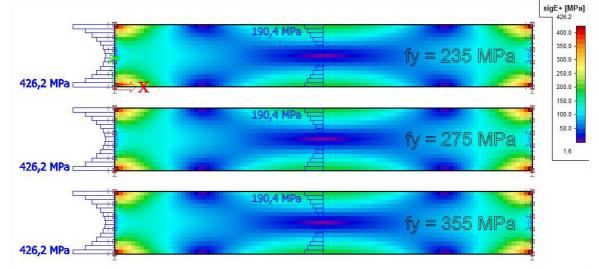
A first indicator is of course if the nonlinear calculation can find a solution. If the stiffness matrix becomes singular when considering general plasticity, the plastic deformations could be so big that the structure becomes a mechanism and no solution is found. The structure cannot hold the loads.

If the calculation succeeds, the check needs to be done on the amount of plastic strain. It can be displayed in the results for 2D stresses, when changing the type of values to basic (in local axis) or principal (in principal axis) plastic strain.



Example: Plastic_Plate_Stresses.esa

In this project, 3 vertical walls of different steel materials are loaded each time by the same vertical surface load of 242.90 kN/m². The value of the load is high enough to make sure that the Von Mises stresses in every wall are higher than the allowed yield strength fy of the steel materials.

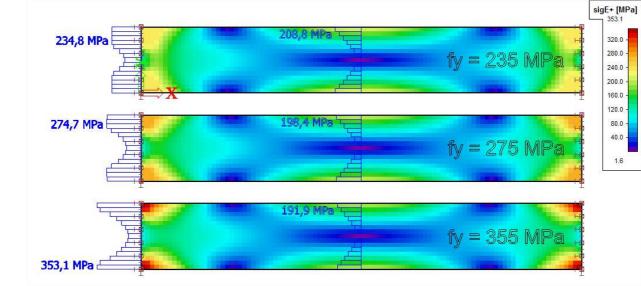


A linear analysis shows the following results for the Von Mises stresses:

As expected, the Von Mises stresses for every wall are exactly the same and are higher than the yield strength fy.

For every used material, the following properties for the nonlinear analysis are inserted:

Material	S		×
# 📲 🗹	📅 📴 🛳 🤌 🛅 🔗 🚘 🕗 🗛	~ T	
S 235	Material type	Steel	^
S 275	Thermal expansion [m/mK]	0,00	
S 355	Unit mass [kg/m^3]	7850,0	
	E modulus [MPa]	2,1000e+05	
	Poisson coeff.	0,3	
	Independent G modulus		
	G modulus [MPa]	8,0769e+04	
	Log. decrement (non-uniform damping only)	0,15	
	Colour		
	Thermal expansion (for fire resistance) [m/mK]	0,00	
	Specific heat [J/gK]	6,0000e-01	
	Thermal conductivity [W/mK]	4,5000e+01	
	Price per unit [€/kg]	1,00	
	 Material behaviour for nonlinear analysis 		
	Material behaviour	Isotropic elasto-plastic, von Mises	~
	Note	ductile materials (metal, steel, aluminium)	
	Input type	Elasto-plastic	*
	Yield stress in uniaxial tension [MPa]	235,0	
	4 EC3		
	Ultimate strength [MPa]	360,0	Y
New In	isert Edit Delete		Close

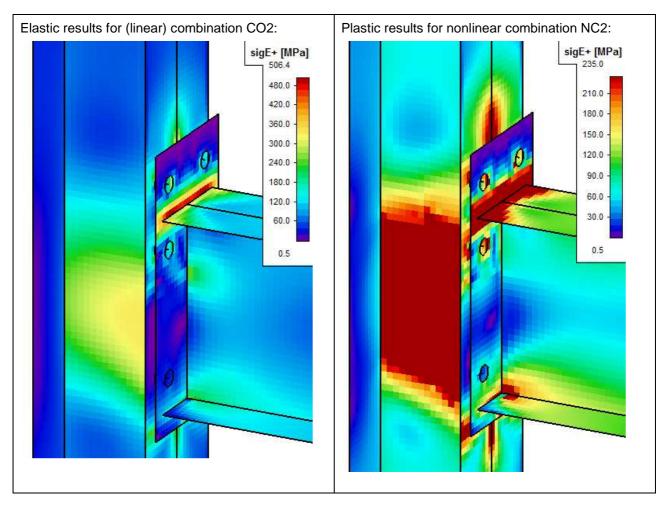


The nonlinear analysis shows the following results for the Von Mises stresses:

Example: Beam_Column_Connection.esa

The functionality **General Plasticity** can also be used to model steel connections using finite elements to perform a plastic stress check.

In this example, a bolted column-beam connection is modelled using 2D finite elements in SCIA Engineer. That way the plastic stresses can be calculated by performing a nonlinear analysis.



Nonlinear Stability

In this final chapter we will combine both the stability and nonlinear effects into a nonlinear stability calculation.

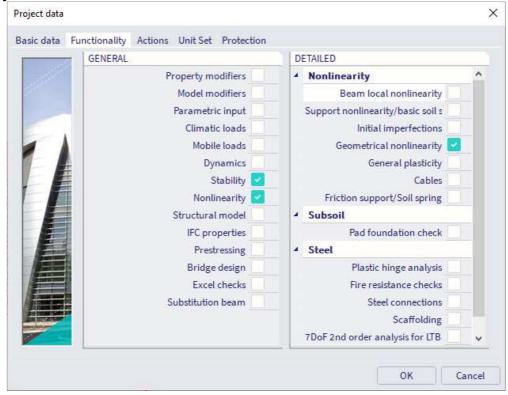
As specified in the assumptions of the first paragraph: a stability calculation is by default a linear process. nonlinearities like friction supports, pressure only supports... are not taken into account. Specifically for this purpose, SCIA Engineer provides the use of a nonlinear stability calculation. This type of calculation has the following additions to the linear stability calculation:

- Local nonlinearities are taken into account
- 3rd order effects are taken into account using the Modified Newton-Raphson algorithm.

Modified Newton-Raphson follows the same principles as the default method but will automatically refine the number of increments when a critical point is reached and will only update its stiffness matrix every N iterations. This method can therefore give precise results for post-critical states.

SCIA Engineer will perform a 3rd order calculation taking into account local nonlinearities. After this calculation, the resulting deformed structure is used for a Stability calculation. As a result, the critical load factor of the structure is obtained for the structure including nonlinearities.

To activate the nonlinear stability calculation, the functionalities **Stability** and **Nonlinearity > geometrical nonlinearity** must be activated.



In addition, support and/or beam local nonlinearities can also be activated.

The choice of the 3rd order theory, the amount of increments and the maximal amount of iterations can be specified in the **solver settings**.

III S	Solver setup		×	
	Warning when maximal rotation is greater than [mrad]	100,0000	^	
	Coefficient for reinforcement	1		
	Print time in Calculation Protocol	~		
	Nonlinearity			
	Geometrical nonlinearity	3rd order (large de 🗸	٦.	
	Method of calculation	Newton-Raphson 👻	I.	
	Number of increments	5	I.	
	Maximum iterations	50		
	Solver precision ratio	1		
	Solver robustness ratio	1		
	Initial stress			
	Initial stress			
	Stability			
	Type of eigen value solver	Subspace iteratior \mathbf{v}		
	Number of buckling modes	1	¥	
A high value of robustness ratio improves the stability of the convergence of nonlinear analysis, but it also slows down the process.				
	8 8 ×	OK Cance	el	
	· · · · · · · · · · · · · · · · · · ·			

Since the nonlinear stability calculation automatically implies the modified Newton-Raphson method for the solver, this method cannot be adapted in the settings. The option is available for the sake of choosing a method for the normal nonlinear calculation.

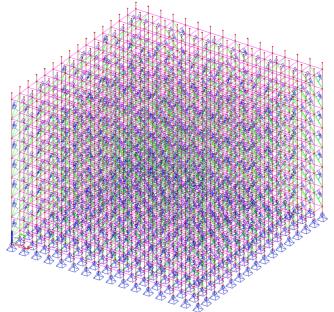
Since the modified Newton-Raphson method also uses load increments, it is important to set a right amount of increments. Therefore it is advised to choose for the Newton-Raphson method, so you can input the number of increments.

The nonlinear stability calculation can then be selected in the calculation window:

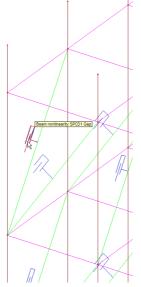
FE analysis	×
Calculations	Mesh setup
Linear analysis	Average number of 1D mesh elements (5
Load cases: 2	Average size of 1D mesh element on cu
Nonlinear analysis Nonlinear combinations: 1	Average size of 2D mesh element [m] 1 Connect members/nodes
Linear stability	Advanced mesh settings
Buckling modes: 1	Solver setup
🗸 Nonlinear stability	Specify load cases for linear calculation
Buckling modes: 1	Specify combinations for nonlinear cal
Other processes	Advanced solver settings
Test input of data	Deve setup
rest input of carta	Run FEM Solver manager
Save project after analysis	Nexis compatibility 🔽
	Nexis results 🔽
	3D mesh test
	Breakpoint before calculation
	Delete results before calculation 🔽
	Skip check for unsupported entities
	Last calculated result version ('default' 21.0.0029.64
Calculate	

Example: Stability_Falsework.esa

In this example, a stability analysis is carried out on a large falsework structure measuring 15m x 15m x 12m.



All diagonals of the structure have been given a gap of 1mm.

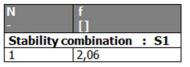


The structure is loaded by its self-weight, formwork and concrete for a total loading of +/- 18.000 tonnes.

First a **linear stability** calculation is carried out to evaluate the critical load factor. The number of 1D elements is set to **5** to obtain good results without severely augmenting the calculation time.

The following result is obtained:

Critical load coefficients



The critical load factor is smaller than 10 which indicates that the structure is susceptible to 2nd order effects. Therefore a 2nd order calculation is carried out using **Timoshenko**. The number of increments is set to **5** and the maximal number of iterations is set to **50**.

The 2nd order calculation leads to the following message:

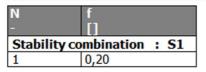
FEM dialog
Calculation Nonlinear
0.01 u fi 0.125 [m] [deg] [deg] 0 0 0 0 FE-Calculation 64 - Warning > The stiffness matrix is singular! The structure is unstable. Instability found in FE-node No. K258, direction X, increment 1.
ОК
Stop after this nonlinear combination No. 1.
Redraw graph Show Data Table
Break Pause

This implies that the 2nd order calculation does not converge to a result but leads to instability. The question now rises as to what causes this instability.

This is the point where the nonlinear stability calculation comes in. During the linear stability calculation, the gap elements on the diagonals of the structure were not taken into account. A nonlinear stability calculation takes into account both 2nd order effects and the gap elements.

The nonlinear stability calculation gives the following result:

Critical load coefficients



This result gives a very important conclusion: the structure including all gap elements is not capable of supporting the loading. Only **20%** of the loading can be supported before instability occurs. This is the reason why the 2nd order calculation does not pass.

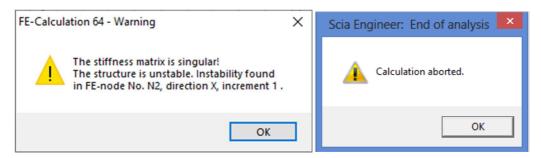
When local nonlinearities are used, it is mandatory to execute a nonlinear stability calculation to draw correct conclusions concerning the global buckling of the structure.

7. Troubleshooting

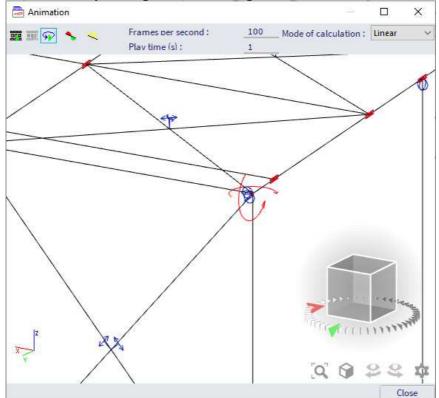
In this final Chapter, some common failure messages are given which can occur during a nonlinear analysis.

7.1 Singularity

Singularity problems occur frequently during a nonlinear calculation. Messages of the following type are generated by SCIA Engineer:



The singularity can be checked by running the check of singularities:

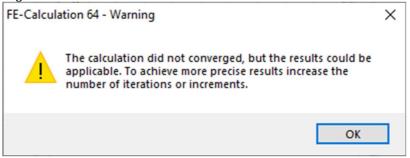


The cause of these messages can be the following:

- The structure is a mechanism: check supports, hinges, unconnected members, ...
- The structure becomes a mechanism by eliminating elements (members, supports, ...) Examples include tension only diagonals which are all eliminated, a subsoil (only compression) which comes entirely under tension, ...
- The structure becomes unstable due to the creation of plastic hinges.
- The entire structure or part of it buckles. In the stiffness matrix this implies that KG > KE
- The instability is caused due to small section properties of manually inputted cross-sections. In many cases, the torsional resistance It is too small.
- As explained in the theory, the Timoshenko method is not suitable when the normal force in a
 member is larger than its critical buckling load. In this case, Newton-Raphson should be applied.
 To find out which cross-section causes this problem, the sections can be modified alternately
 until the 2nd Order calculation passes.

7.2 Convergence

If, during a nonlinear analysis the criterion of convergence is not met, messages of the following type are generated by SCIA Engineer:

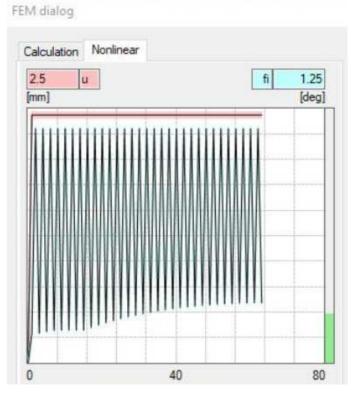


The cause of these messages can be the following:

- Too few iterations have been specified in the Solver Setup.
- The structure is close to instability.
- Cyclic elimination of members or supports: the elements are eliminated during an iteration and are re-instated during the following iteration.
- To examine this in detail, the calculation can be executed for e.g. three iterations: take iteration i-1, i and i+1 and compare the results.
 In these results, there will be a difference in one member (for example in one iteration the member is in tension, in the following iteration it is in compression).
- If the nonlinear stability calculation does not converge, make sure 2nd order (Geometrical Nonlinearity) is activated as functionality.

7.3 Solver robustness ratio

A typical use case for using the robustness ratio is a nonlinear calculation is stuck in some oscillation around the solution value, for instance:



In such a case we would need to "stabilize" the convergence. This can be achieved by slowing down, or dampening the convergence. Let's assume the following:

- iteration 1 gives solution value S1
- in iteration 2, the nonlinear process (e.g. NR) gives solution value S2
- normally, we would just take S2 and continue to the next iteration, but if the values start oscillating wildly, it will not converge
- Instead, we don't take S2 as result of the iteration, but some value in between, using the
 robustness ratio to determine how much of S1 is used in the new solution. An example of this
 (but NOT the formula used in SCIA Engineer) would be:

$$S_2' = \frac{1}{R} \cdot S_2 + \left(1 - \frac{1}{R}\right) \cdot S_1$$

Where R is the robustness ratio. If R=1 it will return standard, non-damped convergence. The higher the value, the more of S1 will be in the solution, the slower the convergence, but the more stable the calculation will be. The actual formula in SCIA is far more complex, but the principle remains the same.

References

- [1] V. Kolar, I.Nemec, V. Kanicky, FEM : Principy a praxe metody konecnych prvku, Computer Press, 1997
- [2] W. Nijenhuis, De Verplaatsingsmethode, 1973
- [3] J. Blauwendraad, A.W.M. Kok, Elementenmethode 2, Agon Elsevier, Amsterdam/Brussel, 1973
- [4] K.J. Bathe, Finite Element Procedures in Engineering Analyis, Prentice-Hall, Inc. Englewood Cliffs, New Jersey, 1982
- [5] J.S. Przemieniecki, Theory of Matrix Structural Analyis, McGraw-Hill Book Company, 1968
- [6] S. P. Timoshenko, J. M. Gere, Theory of elastic stability, McGraw-Hill Book Company, 1963
- [7] Stahl im Hochbau, 14. Auflage, Bandl / Teil 2, Verein Deutscher Eisenhüttenleute, Düsseldorf, 1985
- [8] ESA 3 2de Orde Beton, Raamwerken 2de Orde Theorie Beton, Scientific Application Group S.V., 1981
- [9] Eurocode 3, Design of steel structures, Part 1 1 : General rules and rules for buildings, ENV 1993-1-1:1992, 1992
- [10] FEM 10.2.02, The Design of Steel Pallet Racking, Fédération Européenne de la Manutention, Section X, July 2000
- [11] Eurocode 3 : Part 1.1., Revised annex J : Joints in building frames, ENV 1993-1-1/pr A2
- [12] SCIAESA PT Connect Frame & Grid, Theoretical Background, Release 4.40, SCIA, 04/2004
- [13] Esa Prima Win Connect Frame, Truss Connection, Bolted diagonal connection, Manual, Release 3.30, SCIA, June 2001
- [14] DIN 18800 Teil 1, Stahlbauten : Bemessung und Konstruktion, Beuth Verlag GmbH, Berlin, 1990
- [15] DIN 18800 Teil 2, Stahlbauten : Stabilitätsfälle, Knicken von Stäben und Stabwerken, Beuth Verlag GmbH, Berlin, 1990
- [16] Beuth-Kommentare, Stahlbauten : Erläuterungen zu DIN 18800 Teil 1 bis Teil 4, Beuth, Ernst & Sohn, Berlin, 1993
- [17] U. Kuhlmann, Stahlbau Kalender 1999, Ernst & Sohn, 1999

[18]	M. Braham, E. Lascrompes, L'analyse élastique des ossatures au moyen de l'Eurocode 3, Revue Construction Métallique, n° 4-1992
[19]	Frame design including joint behaviour, Volume 1, ECSC Contracts n° 7210- SA/212 and 7210-SA/320, January 1997
[20]	Ontwerp-handboek voor geschoorde of zijdelings stijve stalen gebouwen volgens EC3, ECCS n° 85, 1996,
[21]	Construction métallique et mixte acier-béton, Calcul et dimensionnement selon les Eurocodes 3 et 4, APK, Eyrolles, 1996
[22]	Esa Prima Win Benchmark PST.06.01 – 07 , Example Code Check and Connections according to EC3 : Design of an industrial type building, SCIA
[23]	NEN 6770, Staalconstructies TGB1990, Basiseisen en basisrekenregels voor overwegend statisch belaste constructies
[24]	NEN 6771, Staalconstructies TGB 1990, Stabiliteit
[25]	EULER : Computerprogramma voor de bepaling van de lineair elastische krachtsverdeling, Eulerse kniklasten en knikvormen van raamwerken, TNO rapport BI-85-1/63.1.0310, Mei, 1985
[26]	Eurocode 3, Design of steel structures, Part 1 - 1: General rules and rules for buildings, EN 1993-1-1:2005.
[27]	Vandepitte D., <i>Berekening van Constructies (Calculation of Structures)</i> , Story- Scientia, Gent, 1979. www.berekeningvanconstructies.be

[28] Höglund T., Beams-Columns, Alternative Imperfection according to Eurocode 9, 2005.